Design and Simulation of a Microturbine Trigeneration System Incorporating Hydraulic Storage and an Inverse Brayton Cycle

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Abstract

Integrated micro-power systems that can provide electricity, heating and cooling (i.e. trigeneration) have the potential to provide greater overall efficiencies than traditional micro-cogeneration power systems with separate cooling devices. With rising grid power rates, small-scale trigeneration has the potential to be economically attractive. The majority of trigeneration systems under development and in use utilize expensive components such as absorption chillers suitable for medium to large-scale trigeneration, which are not economically suitable for small-scale applications.

To bring the economic benefit of trigeneration to small-scale users without incorporating expensive components, an inverted Brayton cycle (IBC) is employed which makes use of the expander section already present in a microturbine. A hydraulic accumulator, indirectly charged by a microturbine, provides pressurized air, which is passed through the expander section of the microturbine and cooled due to expansion; simultaneously providing power and cooling flow. As the microturbine is indirectly fired, the flow passing through the engine or IBC can be directly vented into the household, eliminating the need for additional heat exchangers.
A study was conducted to assess the thermodynamic and economic performance of the proposed system compared to systems currently used, such as individual generation provided by an air conditioner, high efficiency natural gas furnace, and grid power. Simulations were run for a full year based on actual external temperature, electrical, and thermal loads for a single family detached dwelling located in Winnipeg, Canada. The output of the microturbine studied is 10 kWe, suitable for a domestic household, however the system is easily scaled for larger commercial applications. The majority of the components in the system studied are off-the-shelf products. Performance data was generated using MATLAB™ while economic performance was determined with time-based simulations conducted using SIMULINK™. The system allows energy islanding by providing for all household energy needs throughout the year, however integration with a power grid is optional. It was found that the operating costs for the proposed trigeneration system in an energy islanding mode of operation were equivalent to or less than individual generation (air conditioning unit, natural gas furnace, grid power) during heating modes of operation, and more expensive for cooling modes of operation. The yearly energy cost for the trigeneration system exceeded the total cost of running individual systems by 30 to 48 percent, however there remains much room for improvement to the trigeneration concept. All economic data was based upon fair market energy prices found in central Canada.
Acknowledgments

Writing this thesis has been the highlight of my academic career, and has been the most challenging, exciting, and rewarding experience of my life. I could not have achieved the results I did without the guidance and tutelage of my co-supervisors Dr. Donald Gauthier and Dr. Xiao Huang. My gratitude to you both for helping to improve me as an engineer, researcher, and writer.

Special thanks to Marianne Manning of the National Research Council Canadian Centre for Housing Technology in Ottawa, Ontario for providing access to measured thermal and electrical load data. Gratitude is expressed towards Dr. Ian Beausoleil-Morrison, Associate Professor and Canada Research Chair at Carleton University for providing access to ESP-r source code. Financial support was graciously provided by Dr. John Rogers of Innovative Materials Technology (IMT).

Finally, I must thank my wife who selflessly shelved her life in Winnipeg to set up shop in a strange and new land to allow me to pursue my dreams. Any struggles overcome while completing this work were far surpassed by the trials she was forced to endure moving away from family and a career. I couldn’t have done this without you.
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Nomenclature

\[ A_{cyl} \]  
surface area of cylindrical portion of accumulator

\[ A_{sp} \]  
surface area of spherical portion of accumulator

\[ COP \]  
Coefficient of Performance

\[ COP_{nom} \]  
Coefficient of Performance at ARI test conditions

\[ C_{pa} \]  
specific heat of air

\[ \overline{h} \]  
accumulator total free convective heat transfer coefficient

\[ h_{C,in} \]  
heat exchanger cold stream in

\[ h_{C,out} \]  
heat exchanger cold stream out

\[ \overline{h}_{cyl} \]  
heat transfer coefficient for cylindrical portion of accumulator

\[ h_h \]  
household ambient enthalpy

\[ h_{H,in} \]  
heat exchanger hot stream in

\[ h_{H,out} \]  
heat exchanger cold stream out

\[ h_{in} \]  
accumulator inlet enthalpy

\[ h_{out} \]  
accumulator outlet enthalpy

\[ \overline{h}_{sp} \]  
heat transfer coefficient for spherical portion of accumulator

\[ \dot{m} \]  
microturbine mass flow
\( \dot{m}' \) corrected microturbine compressor mass flow

\( m_{\text{acc}} \) accumulator total air mass

\( \dot{m}_C \) heat exchanger cold side mass flow

\( \dot{m}_{c2} \) secondary compressor mass flow

\( \dot{m}_e \) expander mass flow

\( \dot{m}_{e2} \) secondary expander mass flow

\( \dot{m}'_e \) corrected expander mass flow

\( \dot{m}_f \) specific fuel mass flow

\( \dot{m}_f|_f \) natural gas furnace fuel mass flow

\( \dot{m}_H \) heat exchanger hot side mass flow

\( m_h \) mass of air in thermally controlled volume of dwelling

\( \dot{m}_{\text{in}} \) accumulator inlet mass flow

\( \dot{m}_{\text{out}} \) accumulator outlet mass flow

\( P_a \) ambient pressure

\( P_{\text{acc}} \) accumulator pressure

\( \dot{Q} \) microturbine thermal output

\( \dot{Q}_{\text{acc}} \) accumulator thermal output
\( \dot{Q}_{e2} \) secondary expander thermal output
\( \dot{Q}_h \) household thermal load
\( \dot{Q}'_{acc} \) accumulator heat loss
\( R \) universal gas constant
\( T_a \) outside air temperature
\( T_{acc} \) accumulator bulk fluid temperature
\( T_{ground} \) ground temperature
\( T_{in} \) #4 Hx inlet temperature
\( T_{max} \) maximum #2 Hx operating temperature
\( T_{nom} \) ambient temperature at ARI test conditions
\( T_{out} \) #4 Hx exit temperature
\( T_s \) accumulator external surface temperature
\( T_{\infty} \) household ambient temperature
\( u_1 \) control volume internal energy at previous timestep
\( u_2 \) control volume internal energy at current timestep
\( V \) accumulator volume
\( \dot{V} \) secondary compressor volumetric flow rate
\( \dot{W} \) microturbine electrical output
\( \dot{W}_{ac} \) air conditioner work input

\( \dot{W}_{c_2} \) secondary compressor electrical input

\( \dot{W}_{e_2} \) secondary expander electrical output

\( \dot{W}_h \) household electrical load

\( \Delta P_{hx} \) heat exchanger pressure loss

\( \varepsilon \) HEN heat exchanger effectiveness

\( \varepsilon_4 \) #4 Hx effectiveness

\( \eta_c \) compressor isentropic efficiency

\( \eta_{c_2} \) secondary compressor isentropic efficiency

\( \eta_{comb} \) combustion efficiency

\( \eta_f \) natural gas furnace efficiency

\( \eta_m \) mechanical efficiency

\( \eta_e \) expander isentropic efficiency

\( \eta_{e_2} \) expander isentropic efficiency
<table>
<thead>
<tr>
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<th>Definition</th>
</tr>
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<tbody>
<tr>
<td>ACR</td>
<td>Absorption Chiller Refrigeration</td>
</tr>
<tr>
<td>APU</td>
<td>Auxiliary Power Unit</td>
</tr>
<tr>
<td>ARI</td>
<td>Air-Conditioning and Refrigeration Institute</td>
</tr>
<tr>
<td>BPHE</td>
<td>Brazed Plate Heat Exchanger</td>
</tr>
<tr>
<td>CAD</td>
<td>Canadian funds</td>
</tr>
<tr>
<td>CAES</td>
<td>Compressed Air Energy Storage</td>
</tr>
<tr>
<td>CHCP</td>
<td>Combined Heat Cooling and Power</td>
</tr>
<tr>
<td>CHP</td>
<td>Combined Heat and Power</td>
</tr>
<tr>
<td>Cogen</td>
<td>Cogeneration</td>
</tr>
<tr>
<td>COP</td>
<td>Coefficient of Performance</td>
</tr>
<tr>
<td>CPR</td>
<td>Compressor Pressure Ratio</td>
</tr>
<tr>
<td>DG</td>
<td>Distributed Generation</td>
</tr>
<tr>
<td>EPR</td>
<td>Expander Pressure Ratio</td>
</tr>
<tr>
<td>FOD</td>
<td>Foreign Object Damage</td>
</tr>
<tr>
<td>GHG</td>
<td>Greenhouse gases</td>
</tr>
<tr>
<td>GT</td>
<td>Gas Turbine</td>
</tr>
<tr>
<td>HEN</td>
<td>Heat Exchanger Network</td>
</tr>
<tr>
<td>HRSG</td>
<td>Heat Recovery Steam Generator</td>
</tr>
<tr>
<td>Hx</td>
<td>Heat exchanger</td>
</tr>
<tr>
<td>IBC</td>
<td>Inverse Brayton Cycle</td>
</tr>
<tr>
<td>Acronym</td>
<td>Description</td>
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<tr>
<td>---------</td>
<td>-------------</td>
</tr>
<tr>
<td>ICE</td>
<td>Internal Combustion Engine</td>
</tr>
<tr>
<td>IFGT</td>
<td>Indirectly Fired Gas Turbine</td>
</tr>
<tr>
<td>ISO</td>
<td>International Standards Organization</td>
</tr>
<tr>
<td>kWe</td>
<td>kilowatts electrical power output</td>
</tr>
<tr>
<td>kWt</td>
<td>kilowatts thermal output</td>
</tr>
<tr>
<td>LHV</td>
<td>Lower Heating Value</td>
</tr>
<tr>
<td>LiBr</td>
<td>lithium bromide</td>
</tr>
<tr>
<td>MCFC</td>
<td>Molten Carbonate Fuel Cell</td>
</tr>
<tr>
<td>MWe</td>
<td>megawatt electrical power output</td>
</tr>
<tr>
<td>PFHE</td>
<td>Plate fin Heat Exchanger</td>
</tr>
<tr>
<td>PR</td>
<td>Pressure ratio</td>
</tr>
<tr>
<td>RSI</td>
<td>R-value Système International</td>
</tr>
<tr>
<td>SMMT</td>
<td>Setpoint Min-to-Max Time</td>
</tr>
<tr>
<td>SOFC</td>
<td>Solid Oxide Fuel Cell</td>
</tr>
<tr>
<td>SOFC-GT</td>
<td>Solid Oxide Fuel Cell – Gas Turbine</td>
</tr>
<tr>
<td>STHE</td>
<td>Shell and Tube Heat Exchanger</td>
</tr>
<tr>
<td>STP</td>
<td>Standard Temperature and Pressure</td>
</tr>
<tr>
<td>TELR</td>
<td>Thermal-to-Electrical Load Ratio</td>
</tr>
<tr>
<td>TIT</td>
<td>Turbine (Expander) Inlet Temperature</td>
</tr>
<tr>
<td>Trigen</td>
<td>Trigeneration</td>
</tr>
<tr>
<td>UPS</td>
<td>Uninterruptible Power Supply</td>
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</table>
VCR

Vapour Compression Refrigerator
Chapter 1
Introduction

1.1. Background

Often interesting and useful technologies are never fully explored due to unfavourable market conditions. This was especially true for energy conversion innovation, as the cost of improvements to cycle efficiencies had to compete with long payback periods due to low energy prices. This has changed with recent increases in fuel prices and projected shortages of natural gas in the near future. Value-added technologies such as cogeneration that offer multiple energy products have received greater attention and acceptance through validation and operation in industrial environments. Improvements to energy conversion efficiencies were initially the concern of large businesses, however these concepts have drawn the interest of small-scale users as well. There is an interesting opportunity to bring value-added energy solutions to the general consumer, one such technology that shows promise is trigeneration (also known as trigen or combined heat, cooling, and power (CHCP)). Typical trigeneration systems currently found in industry use either a vapour compression cycle or an absorption chiller (ACR) [1.1][1.22][1.45], as illustrated in Figure 1-1 and Figure 1-2. As such systems require installation of a refrigeration unit in addition to a heat recovery steam generator (HRSG), the specific capital cost requirements
cannot be justified for small-scale generation.

Figure 1-1: Cycle diagram for typical industrial CHCP based on a gas turbine and an absorption chiller cycle

Figure 1-2: Cycle diagram for a typical industrial CHCP based on a gas turbine and a vapour compression refrigeration system.
To introduce trigeneration to the small-scale consumer, a cycle that eliminates the need for expensive subsystems is required. Another key factor contributing to an increasing interest in distributed generation (DG), cogeneration and trigeneration (CHP and CHCP) for the small-scale consumer is the unreliable nature of many power grid systems. As power utilities in major urban centres such as Southern California and the Eastern United States seaboard continue to operate close to grid capacity, brownouts and blackouts will most likely become more frequent. A number of companies with sensitive financial and identity data such as CitiBank and JP Morgan have already installed emergency backup power systems [1.30]. However for a small-scale consumer, the overhead involved in purchasing and operating a backup power system is often too high. Combining power generation with cooling and/or heating load production is most likely the only way such a system can be economically attractive to small-scale customers.

Increasing demand for legislation focused on reducing greenhouse gases has resulted in favourable environments for DG and CHP in many regions nations around the world. California, Texas and most European countries have created cash incentives for cogen systems that demonstrate a reduction in controlled emissions over conventional energy systems, and meet target thermal efficiencies [1.4]. By rewarding efficient cogen systems with cash incentives,
small-scale DG becomes more economically attractive. While legislation does not cover trigeneration systems at present, it is anticipated this will change as trigen market penetration increases.

1.2. DG, CHP, and CHCP market outlook

In North America, power is provided by a few utilities that, in many cases, enjoy regional monopolies. This proves to be a significant deterrent for distributed power, as electric utilities have traditionally made it hard or impossible for excess DG power to be sold back to the grid. Looming shortfalls in grid power supply in major urban centres along the North American coasts motivated local governments to put pressure on major utilities to begin creating favourable environment for distributed power generation [1.31]. In addition to reducing load on the main grid, it has been suggested that DG has the potential to not only provide stability via decentralization, but to improve power quality and transmission efficiency [1.5]. With regulatory roadblocks falling away, and current micro-generation technology sufficiently developed for commercial and industrial implementation, it is anticipated small-scale DG, CHP, and CHCP will achieve greater market penetration.

The key to achieving small-scale DG, CHP, or CHCP penetration is in driving capital investment costs down. As the major focus of generation efforts has been
in the megawatt (MW) scale, specific capital costs rise as the output decreases; shown in Figure 1-3. Achieving a small-scale DG, CHP, or CHCP system that has reasonable specific capital costs cannot be accomplished by simply scaling down large engine technology. A technically and economically successful system will be designed from the ground up, specifically targeting the less than 50 kWe range. Distributed CHP plants in this range have received commercial acceptance in California and Japan; evident by the existence of significant contributors to the microturbine CHP market such as Capstone Turbines in Chatsworth, CA and Ebara Corp. in Japan. However, rising fuel costs compared to minor electric rate increases have prevented significant penetration of CHP and CHCP technologies into the less than 50 kW market.

![Figure 1-3: Specific capital costs of medium to large cogeneration systems](image)

**Figure 1-3:** Specific capital costs of medium to large cogeneration systems [1.7]
Figure 1-4: Capacity of commercial CHP by application in the United States (2000) [1.39]

As mentioned previously, the power distribution regulatory environment is becoming less hostile and, in fact, favourable towards small-scale distributed CHP. Despite this, current small-scale CHP technologies less than 50 kW face severe economic challenges. Figure 1-4 illustrates this fact as small-scale facilities such as restaurants and food stores account for only 0.13 percent of total commercial CHP production in the United States [1.39]. With reference to Table 1-1, small commercial users such as restaurants, golf clubs, spas, car washes, and laundromats represent a CHP potential of 9748 MW [1.39]; this data does not include potential from the residential sector, making potential small-scale CHP estimates strongly conservative. This is a large market that has very little incentive to switch to a CHP or CHCP system given the products currently
on the market. Consumers are becoming more eco-aware when making purchase decisions. The ecological benefits of trigeneration combined with the lack of small-scale systems available make the market potential enormous for a trigen system that can perform well ecologically and economically.

Table 1-1: Comparison of existing CHP to potential CHP supplied in the United States [1.39]

<table>
<thead>
<tr>
<th>Application</th>
<th>Total Potential (MW)</th>
<th>Installed CHP (MW)</th>
<th>Remaining Potential (MW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hotels/Motels</td>
<td>6,703</td>
<td>30</td>
<td>6,673</td>
</tr>
<tr>
<td>Nursing Homes</td>
<td>7,993</td>
<td>11</td>
<td>7,982</td>
</tr>
<tr>
<td>Hospitals</td>
<td>8,878</td>
<td>491</td>
<td>8,387</td>
</tr>
<tr>
<td>Schools</td>
<td>14,884</td>
<td>14</td>
<td>14,870</td>
</tr>
<tr>
<td>Colleges/Universities</td>
<td>4,250</td>
<td>1,414</td>
<td>2,836</td>
</tr>
<tr>
<td>Commercial Laundries</td>
<td>485</td>
<td>3</td>
<td>482</td>
</tr>
<tr>
<td>Car Washes</td>
<td>281</td>
<td>0</td>
<td>281</td>
</tr>
<tr>
<td>Health Clubs/Spas</td>
<td>3,552</td>
<td>164</td>
<td>3,388</td>
</tr>
<tr>
<td>Golf Clubs</td>
<td>2,208</td>
<td>0</td>
<td>2,208</td>
</tr>
<tr>
<td>Museums</td>
<td>398</td>
<td>4</td>
<td>394</td>
</tr>
<tr>
<td>Correctional Facilities</td>
<td>2,721</td>
<td>135</td>
<td>2,586</td>
</tr>
<tr>
<td>Water Treatment/Sanitary</td>
<td>949</td>
<td>141</td>
<td>808</td>
</tr>
<tr>
<td>Extended Service Restaurants</td>
<td>3,390</td>
<td>1</td>
<td>3,389</td>
</tr>
<tr>
<td>Supermarkets</td>
<td>1,184</td>
<td>0</td>
<td>1,183</td>
</tr>
<tr>
<td>Refrigerated Warehouses</td>
<td>792</td>
<td>0</td>
<td>792</td>
</tr>
<tr>
<td>Office Buildings</td>
<td>18,614</td>
<td>235</td>
<td>18,379</td>
</tr>
<tr>
<td>Other</td>
<td>N/A</td>
<td>2,282</td>
<td>N/A</td>
</tr>
<tr>
<td>Total</td>
<td>77,282</td>
<td>4,926</td>
<td>74,638</td>
</tr>
</tbody>
</table>

1.3. Applications of DG, CHP, and CHCP

1.3.1. Emergency power

A very limited use for a DG system is for backup or emergency power. Such
systems have been sold on both large and small scales for decades; typically small-scale units have been restricted to spark ignition or compression ignition engines while larger units have made use of gas turbine generator sets. IHI corp. located in Japan has drawn on Japanese microturbine expertise to produce a mobile 2.6 kW microturbine emergency generator seen in Figure 1-5.

Many industries cannot afford to stop services or production due to power failures. Often the high cost of installing a backup power system, outweighs the cost of just one power failure. Table 1-2 shows the motivation behind installing emergency power systems, despite the significant capital required for what seems like a minimal return. When generating emergency power, cycle efficiencies and fuel consumption are not the primary concern since the system operates several hours a year, as opposed to 24-7 operation as in a baseload mission.

<table>
<thead>
<tr>
<th>Industry</th>
<th>Average downtime costs (USD/hr)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cellular Communications</td>
<td>41,000</td>
</tr>
<tr>
<td>Telephone ticket sales</td>
<td>72,000</td>
</tr>
<tr>
<td>Airline reservations</td>
<td>90,000</td>
</tr>
<tr>
<td>Credit card operations</td>
<td>2,580,000</td>
</tr>
<tr>
<td>Brokerage operations</td>
<td>6,480,000</td>
</tr>
</tbody>
</table>

CHP and CHCP systems are not designed for emergency power systems, as the
increased specific capital cost required to install them cannot be recovered if the
system operates only during emergencies. Small-scale users typically do not
purchase emergency power systems, as the cost of losing power is usually
negligible. An economically successful small-scale trigeneration system cannot
be incorporated as part of existing backup power technology, as a trigeneration
system must operate for a significant portion of the year to be economically
competitive.

Figure 1-5: IHI Dynajet 2.6 microturbine powered portable generator [1.15]

1.3.2. Vehicles

In addition to requiring propulsion, many vehicles require high electrical and
thermal loads. If the vehicle is large enough, these loads are often satisfied with a secondary powerplant. For example, auxiliary power units (APU) are installed on medium to large aircraft as shown in Figure 1-6.

Figure 1-6: Honeywell APU installed in a B737 [1.29]

These small turboshaft gas turbines satisfy thermal and electrical loads while on the apron or during taxi. Unfortunately the overall thermal efficiency of APU trigeneration is very poor. This is partially due to the fact that the thermal load
provided by the APU is always in excess of what is required by the aircraft; the excess is dumped overboard. There is little motivation to improve this process as the APU is in operation for a small fraction of aircraft operating hours and represents an even smaller fraction of fuel consumption when compared to the consumption of the main engines. While there is much to be learned from APU-based trigeneration, it is clear that terrestrial small-scale users require a different trigeneration system to be economically successful.

An interesting parallel can be made between large ocean vessels employing a CHP system, and a small-scale user. An ocean vessel requires much the same services as a residential customer or a small business: food preparation, laundry, lighting, environmental heating, and process heat, to name a few. Often these loads are satisfied with either a separate dedicated system, or are supplied by the main powerplant; creating a hybrid CHP system. Traditionally such loads were satisfied using a main boiler. Many vessels still use one, however marine cogen has been used in new construction as early as the late 1970s [1.24]. As reducing specific fuel consumption is of primary concern on a marine vessel, the technology developed for marine use should be of particular interest for land-based CHP users; key lessons and cycle innovations developed to save fuel, and system size can help to make a small-scale DG system more attractive to consumers. A significantly different system is required for small-scale land-based
consumers as marine systems are not capable of trigeneration at the present time. In addition, the specific capital cost of marine cogen systems is too high for small-scale users. A new trigen system that does not use boilers, absorption chillers, or other components oriented towards the large-scale user is required.

1.3.3. Energy islanding

For applications where grid power is either inconsistent or non-existent, efficient cost effective energy islanding is required. Northern Canadian communities are often powered by spark ignition or compression ignition engines and heat is provided using electric baseboards or a wood stove. Portable reciprocating engine generators are prone to maintenance issues, and do not make use of exhaust heat. The emissions from these generators, particularly from compression ignition engines, have high concentrations of unburnt hydrocarbons (UHC) and soot. Such communities are prime candidates for a power generation and heating system that can be provided with a small-scale trigen package.

It is not only remote communities that can take advantage of such solutions; industries with mobile applications such as the oil and gas industry, military organizations, can benefit from the mobile high power density offered by microturbines. With respect to a military application, recuperated microturbines are an attractive DG solution in a combat role; low exhaust temperature and
noise signatures help reduce the chance of detection from infrared seeking equipment and munitions.

Energy islanding has the potential to be attractive for small-scale users with grid power access as well. For customers where power service is routinely disrupted due to inclement weather or due to a weak grid, and for customers where natural gas service is not available, DG systems are an attractive solution to eliminating service disruption and high heating costs. Table 1-3 shows the total energy consumption for Canadian households for the purpose of space heating for 2000 to 2004. Note that while the majority of Canadians use natural gas for space heating, 45.4 percent of the total energy used for space heating did not come from natural gas, presumably due to lack of access and the use of older heating technology. It is also interesting to note that electricity use increased from 2000 to 2004 while natural gas use did not change. This suggests that more people are living in areas without natural gas access, where space heating can only be accomplished with expensive alternatives such as electric heat, oil furnaces, or wood stoves. These statistics indicate that total or partial energy islanding has the potential to become increasingly attractive to small-scale users, however an economically viable small-scale CHP/CHP package is not available on the market.
Table 1-3: Canadian space heating energy consumption statistics, presented in petaJoules [1.27]

<table>
<thead>
<tr>
<th>Year</th>
<th>Electricity</th>
<th>Natural Gas</th>
<th>Heating Oil</th>
<th>Other</th>
<th>Wood</th>
</tr>
</thead>
<tbody>
<tr>
<td>2000</td>
<td>140.6</td>
<td>445.0</td>
<td>115.4</td>
<td>11.9</td>
<td>101.2</td>
</tr>
<tr>
<td>2001</td>
<td>134.0</td>
<td>404.8</td>
<td>104.4</td>
<td>11.9</td>
<td>94.7</td>
</tr>
<tr>
<td>2002</td>
<td>142.0</td>
<td>437.6</td>
<td>100.9</td>
<td>11.5</td>
<td>100.1</td>
</tr>
<tr>
<td>2003</td>
<td>153.6</td>
<td>460.2</td>
<td>106.7</td>
<td>11.5</td>
<td>104.7</td>
</tr>
<tr>
<td>2004</td>
<td>157.2</td>
<td>442.9</td>
<td>92.7</td>
<td>11.6</td>
<td>106.8</td>
</tr>
<tr>
<td>percent change 2000-2004</td>
<td>10.6</td>
<td>-0.5</td>
<td>-19.7</td>
<td>2.5</td>
<td>5.2</td>
</tr>
</tbody>
</table>

1.3.4. Peak shaving

To encourage customers to distribute power consumption throughout the day, and to recover costs associated with operating ‘peaking’ plants, many utilities charge peak rates during high consumption periods. This has resulted in the use of DG as a cost-reduction strategy. As many DG systems are too costly to run when competing with off-peak electricity prices, optimization strategies often include operating a DG system only once a minimum electrical tariff is exceeded [1.2][1.16][1.20]. Most DG systems installed for the purpose of peak shaving do not include CHP or CHCP cycles, as the extra cost associated with such systems cannot be recovered if the system operates for only a portion of the day. Peak shaving had become so popular by the turn of the century that gas turbine gensets in the 3 to 65 MW range are in short supply [1.33]. This trend in grid decentralization can only be expected to continue if electricity peak tariffs continue to climb. For a small-scale user who typically consumes 5 to 8 kW at
peak load (for a single family detached household) [1.11], peak shaving DG systems do not make economical sense.

1.3.5. Process heat and cooling

Many industrial processes require large amounts of heating and/or cooling load. This load is traditionally generated using boilers (heat load) or chiller technology fired by natural gas or powered with electricity (cooling load). As energy contained in high-temperature exhaust is not utilized, traditional generation of process energy has a lower thermal efficiency compared to cogen or trigen systems.

California DG and CHP standards are seen as the model for the rest of North America who typically follow suit. The California Energy Commission's Distributed Generation and Cogeneration Policy Roadmap outlines a strategy currently being implemented through 2020 to increase DG and CHP market penetration in California to 25 percent of total peak demand [1.31]. To do this, the commission indicates that among other incentives and regulatory requirements, a continued effort to "remove institutional barriers" is essential for DG and CHP success. This is described as making permits easier to obtain, and to provide assistance for integrating DG into the main grid efficiently. With such a favourable regulatory climate, generating process heat and cooling load is much
more attractive for large-scale industrial users and small-scale users alike. Historically it was very difficult to sell overproduction of electrical power from CHP and CHCP back to the grid, and still remains so in some areas of North America. This overproduction represented a ‘virtual penalty’ on overall efficiency, as any energy not used on site was ‘dumped overboard’. By being able to generate an income from overproduction, the overall efficiency of a CHP or CHCP system is increased, and an additional income source is generated to offset fuel costs. It can only be anticipated that as peak loads become more of a concern around North America and the world, the DG and CHP framework being established by California will serve as a model for encouraging the growth and economic viability of trigeneration systems.

1.4. Small-scale CHP and CHCP technology
There are several technologies to choose from when designing a small-scale CHP or CHCP system. As there are pros and cons to all of them, the following will give a brief overview of which system is best suited for small-scale CHP or CHCP.

1.4.1. Reciprocating engines
Commonly referred to as diesel or gasoline engines, these reciprocating prime movers are often seen in an emergency/backup DG role. Diesel generators have
been used in peaking plants and other non-baseload environments as well, however gasoline engines have not seen the same use outside of small-scale emergency power generation and CHP. Some have experimented with small-scale (less than 15 kW) CHCP and CHP systems involving diesel or gasoline prime movers [1.20][1.22][1.25]. Thermodynamically speaking these systems are good performers with overall efficiencies of 70 to 80 percent, however these studies do not take into consideration maintenance and reliability issues. The biggest weakness of the reciprocating engine is high maintenance costs. Table 1-4 is a high-level comparison of typical maintenance and overhaul costs for four key powerplant CHP and CHCP systems in the 5 to 100 kW electrical output range. This may come as a surprise as most relate to reciprocating engines via experience gained from operation of cars or trucks, which require routine maintenance roughly once a year. In this context, reciprocating engines can last 10 to 15 or more years before major overhaul.

Table 1-4: Typical maintenance costs for prime mover CHP and CHCP technologies [1.19]

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Typical maintenance</td>
<td>0.008-0.015</td>
<td>0.007-0.018</td>
<td>0.002-0.010</td>
<td>0.023</td>
</tr>
<tr>
<td>costs (USD/kWh)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

However the duty cycle during this time is different when compared to a CHP or
CHCP environment: operation of a vehicle 2 to 3 hours a day for 10 years results in 7300 to 11000 hours of operation. A generator, CHP, or CHCP prime mover will typically operate the majority of the day resulting in 6500 to 7000 hours of operation per year or 6 to 10 times longer over a 10 year period, when compared to a reciprocating engine operating in a vehicle powerplant mission.

Figure 1-7: Existing reciprocating engine CHP in the United States (2002) [1.8]

A typical small-scale user is not interested in keeping a rigid maintenance schedule and does not employ maintenance personnel to monitor the health of
system components. When gasoline and diesel engines are employed in a large-scale DG, CHP, or CHCP environment, the user will most likely employ a power engineer or equivalent to monitor the health and maintain reliability of reciprocating equipment; this is not an option for small-scale users with few employees. As can be seen from Figure 1-7, customers who make use of a reciprocating engine for CHP purposes typically do not have operations in the MW scale.

In addition to maintenance scheduling and cost issues for the small user, noise is also a problem. Reciprocating engines demonstrate steady state operation noise levels in excess of 100 dBA \[1.19\]. At this level, the Canadian Centre for Occupational Health and Safety recommends unprotected exposure not to exceed 15 to 30 minutes a day \[1.3\]. While such noise levels may be acceptable for a facility that can segregate the engine from occupied areas, small users cannot afford the luxury of unusable noise polluted space.

### 1.4.2. Stirling engines

Despite being first patented in 1816 \[1.46\], engines using the Stirling cycle have not received the same fame as its younger counterpart the Otto cycle (patented in 1887) \[0\]. While the ideal Stirling cycle is closer to Carnot cycle efficiencies, in
reality it is on par with Brayton and Otto cycles due to problems with piston sealing and regenerator effectivities of less than unity. The Stirling engine uses a closed cycle with a constant temperature heat addition and removal joined by constant volume processes. In an alpha type Stirling engine, two pistons are joined to a crankshaft. One cylinder is heated and the other is cooled. As the fluid in the hot cylinder expands during constant temperature heat addition, the cold cylinder is driven upwards. This forces cold fluid into the hot cylinder, which then draws the hot piston upwards due to contraction of the cooled fluid. Figure 1-8 gives a diagrammatic representation of a production 50 kW Stirling engine produced by STM Power based in the United States.
The Stirling engine demonstrates unproven potential to penetrate the less than 15 kW small-scale CHP market. The combination of low noise signature and small package are attractive to consumers looking for either energy islanding or a supplement to the grid. WhisperGen™, a company in New Zealand, will be introducing a Stirling engine to the European market in 2009 capable of providing 1 kW of electrical output and up to 12 kW thermal output (in the form of hot water) [1.42].

Purchase price and maintenance costs are still unavailable with which to make an economic comparison with other CHP and CHCP technologies. Historical data on Stirling engines suggest maintenance costs are slightly better than reciprocating engines but still above microturbines (see Table 1-4). Several companies have developed Stirling engines for use in packaged CHP applications including: SOLO in Germany, WhisperGen™ in New Zealand, and STM Power from the United States. With the exception of WhisperGen™, all other commercial Stirling CHP packages are targeted for 50 kWe or greater industrial use. Perhaps this is due to the high specific capital cost ($/kW) Stirling engine packages have demonstrated. Very conservative estimates place the procurement price of a Stirling CHP package at 3400 USD/kW. A typical North American household requires about 5 kWe at peak demand [1.23], resulting in an estimated 17,000 USD price tag (not including installation) for a small-scale
residential Stirling CHP unit. Considering a high-efficiency furnace can be purchased for 3,000 to 4,000 USD [1.6], Stirling powered small-scale cogen has some significant economic hurdles to overcome in order to achieve market success.

1.4.3. Microturbines

Perhaps the most promising powerplant technology currently available for small-scale trigeneration are microturbines. Having benefited from significant government research and development funding in the United States, microturbines are evolving from being classified as experimental to now being widely accepted as an established technology. The Advanced Microturbine System [1.40] and Microturbine Materials Technology [1.44] programs run by the US Department of Energy have stated objectives to increase the thermal efficiency of microturbines to 40 percent, making it possible for microturbine systems to surpass the efficiencies of small-scale reciprocating engine systems while maintaining reliability. The microturbine is a particularly robust system as there is only one moving part: the main rotor as seen in Figure 1-9. The result is a technology similar to household furnaces; the consumer is aware it is operating, but is not required to carry out any maintenance. As DG microturbine systems have been in operation since the early 90s, maintenance periods and service life claims have moved from estimates to being supported with field data.
For example, Appendix D contains actual maintenance intervals for the Capstone Turbines 60 kWe C60 and C65 DG microturbine.

![Figure 1-9: Cutaway view of a microturbine](image)

Compare this with reciprocating engines, which require the cylinder head and head gasket to be overhauled at 10,000 hour intervals, and demonstrate a useful life of 30,000 hours [1.8]. Stirling engines with an output of less than 15 kW designed for use in CHP are new to the market and have not accumulated data on reliability and maintenance as of yet. Based upon historical and current experimental data, Stirling CHP systems would most likely require significant routine maintenance at 4,000 to 6,000 hours of operation [1.19]; roughly one
quarter of the demonstrated 20,000 hour interval for a microturbine (see Appendix D). Estimates for useful life vary wildly for Stirling engines due to a lack of historical data to draw from, therefore it is prudent to leave the useful life of a Stirling powered DG or CHP system as unknown at this point.

Table 1-5: Quantitative comparison of potential small-scale DG/CHP/CHCP powerplants (less than 50 kW). This data represents a conservative average from the following sources: [1.8] [1.9] [1.10] [1.19] [1.32] [1.39] [1.40] [1.41]

<table>
<thead>
<tr>
<th></th>
<th>Microturbine</th>
<th>Stirling</th>
<th>Reciprocating</th>
<th>SOFC-GT</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Electrical efficiency (percent)</strong></td>
<td>25-30</td>
<td>20-35</td>
<td>30-35</td>
<td>60+</td>
</tr>
<tr>
<td><strong>CHP Thermal efficiency (percent)</strong></td>
<td>71-86</td>
<td>80-89</td>
<td>~80</td>
<td>N/A</td>
</tr>
<tr>
<td><strong>Specific Capital Cost (USD/kW)</strong></td>
<td>500-650</td>
<td>3400+</td>
<td>550-700</td>
<td>2850++</td>
</tr>
<tr>
<td><strong>Maintenance Cost (USD/kW)</strong></td>
<td>0.002-0.010</td>
<td>0.008-0.015</td>
<td>0.007-0.018</td>
<td>0.023</td>
</tr>
<tr>
<td><strong>Operating noise (dBA) @ 3ft</strong></td>
<td>57-82</td>
<td>50-75</td>
<td>100+</td>
<td>60 (@ 10 m)</td>
</tr>
<tr>
<td><strong>Maintenance intervals (khr)</strong></td>
<td>~11</td>
<td>4-6</td>
<td>8-10</td>
<td>2-4</td>
</tr>
<tr>
<td><strong>Major Overhaul (khr)</strong></td>
<td>45+</td>
<td>?</td>
<td>&lt;30</td>
<td>24</td>
</tr>
</tbody>
</table>

As microturbine machinery is very simple with only one moving part, maintenance costs are very low. Mechanical simplicity also results in low specific capital costs. With reference to Table 1-5, it can be seen that the microturbine
offers the lowest operational and startup cost of the three options discussed thus far (SOFC-GT systems will be discussed in Section 1.4.3.4). In the case of CHCP, a successful system has to compete with highly efficient individual generation provided by a vapour compression air conditioner, natural gas furnace, and grid power. To do so, low specific capital and maintenance costs are vital. The same can be applied to small-scale DG and CHP systems as consumers requiring less than 50 kW of electrical power cannot afford the capital required for a Stirling system, nor the maintenance costs of a reciprocating system.

As discussed in Section 1.4.1, a successful DG, CHP, or CHCP system targeted for the small-scale user must demonstrate low operational noise. Table 1-5 compares operating noise levels of competing small-scale powerplants; it can be seen that the microturbine operates within an acceptable noise range. For comparison, the average clothes dryer operates at 60-75 dBA [1.17]. This combination of minimal maintenance, high reliability, and low operating noise ensures that a microturbine trigeneration system is 'out of sight and out of mind'.

1.4.3.1. Available CHP microturbine packages

There has been substantial research and development effort made in the 50 to 150 kW range for microturbine-powered CHP. As a result, there are several
commercial products currently available for purchase, Table 1-6 summarizes performance data for the more prominent systems. Despite the selection available in the 50 to 150 kW range, there are no microturbine CHP products available below 50 kW. On a cold winter day, a typical Canadian single family detached dwelling will require roughly 10 to 15 kW of heat load with anywhere from 50 W to 8 kW of electrical load [1.11]. CHP systems on the market are not sized to meet such a low demand.

Table 1-6: Market survey for microturbine CHP systems (50 to 150 kW)

<table>
<thead>
<tr>
<th>Manufacturer</th>
<th>Product Name</th>
<th>Electrical Output (kW)</th>
<th>Thermal Output (kW)</th>
<th>Heat Delivery System</th>
<th>Overall Efficiency (percent)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Capstone</td>
<td>C6XICHP [1.34]</td>
<td>65</td>
<td>120</td>
<td>Water</td>
<td>71-82</td>
</tr>
<tr>
<td>Ebara/Elliott</td>
<td>TA100 [1.18]</td>
<td>95</td>
<td>172</td>
<td>Water</td>
<td>74</td>
</tr>
<tr>
<td>Turbec/ABB</td>
<td>T100 [1.37]</td>
<td>100</td>
<td>155</td>
<td>Water</td>
<td>77</td>
</tr>
</tbody>
</table>

1.4.3.2. High-speed generators

A key enabling technology for small-scale microturbine DG, CHP, and CHCP systems is the development of high-speed generators. A high-speed generator uses a permanent magnet mounted directly on the rotor shaft, as seen in Figure 1-10, which allows the generator to operate at speeds of greater than 450,000 RPM. By incorporating the generator as an intrinsic part of the rotor, a gearbox is not required. This eliminates generator-related maintenance, increases the life of the system, and improves efficiency due to negligible mechanical losses in the
high-speed generator as opposed to significant losses in a gearbox. Another benefit of incorporating high-speed generators into microturbines is the reduction in cost that comes with eliminating a gearbox and bulky conventional generator. High-speed generators help to contribute to the autonomous operation of microturbines; no gearbox inspections or gearbox fluid changes translates to less system maintenance, an essential requirement for the unskilled small-scale user.

Figure 1-10: High speed generator permanent magnet rotor shaft [1.37]

1.4.3.3.Zero-lubrication bearings

Bearings have a large effect on turbomachinery life and reliability. Oil degradation, metal flakes, and lubrication coverage issues are some of the major sources of flaking, fatigue, and spalling in lubrication based bearing systems. An oil cooler, reservoir, and pump must be installed as well which only adds to the
complexity and cost of the system; hence it is highly desirable to eliminate the need for a lubrication system.

Air bearings have significant potential for microturbines in that they eliminate the need for an oil distribution system, and improve component life. The air bearing system along with high-speed generators are enabling technologies for microturbines that contribute to the minimal maintenance and long service life demonstrated. An air bearing uses pressurized air forced through very small gaps between stationary and rotating components, effectively ‘floating’ the rotating component without any physical contact.

Figure 1-11: Schematic of a magnetic bearing [1.37]
Magnetic bearings are a more recent addition to the field of non-contact bearing systems. Figure 1-11 shows one particular design by Synchrony, a leader in incorporating magnetic bearings into turbomachinery systems. It can be seen that the rotating shaft floats between the inner magnets and outer magnets, preventing wear due to contact from occurring.

1.4.3.4. SOFC-GT hybrid systems

An interesting addition to the list of potential trigeneration powerplants is the combination of fuel cell technologies with microturbines. The most popular fuel cells used for such an application are the solid oxide fuel cell (SOFC) and the molten carbonate fuel cell (MCFC), as the exhaust from such cells can be as high as 700°C [1.13]. While this temperature may seem low for microturbine applications (a typical microturbine TIT is between 800 and 900°C), the microturbine is only used as a bottoming cycle; any electrical load generated by the microturbine contributes to the efficiency of the system as no extra fuel is injected into the SOFC exhaust. Both the SOFC and microturbine produce electrical load with fuel being added to the SOFC alone. Figure 1-12 illustrates one version of the SOFC-GT being developed by the National Fuel Cell Research Centre in California (NFCRC). These systems show great promise with demonstrated overall electrical efficiencies of 60 percent, and projections of 80 percent in the near future [1.32].
Despite demonstrating very high thermal efficiencies, and exhibiting great potential for emissions reduction, the extremely high specific capital (2850 USD/kW) and maintenance costs (0.023 USD/kWh) make SOFC-GT systems unrealistic for small-scale trigeneration [1.10]. Another limiting factor for SOFC-GT systems is poor transient response time. Fuel cells require warm-up times and cannot be rapidly throttled. For a small-scale load pattern that typically demonstrates rapid variation in load, the SOFC-GT would not be able to operate
in a load following manner. No commercial SOFC-GT units are in operation currently as this technology is still under development, however with the results obtained so far by NFCRC and Siemens (formerly Westinghouse) shows great promise for medium to large-scale DG or CHP applications.

SOFC-GT systems have very low thermal-to-electric load ratios (TELR). This is inverse to what is required in a typical small-scale application that demonstrates TELR values of 4 to 5 [1.23]. To meet a small-scale thermal load, significant overproduction of electrical load is required. Unless this load can be sold back to the grid, this overproduction represents a penalty on overall efficiency no matter how efficiently it was produced.

1.4.4. Thermal storage

Thermal loads for both small- and large-scale applications typically have periods of peak consumption, and periods of low consumption. Sizing a system based on peak consumption can result in poor performance during off-peak hours. Thermal storage offers a way to overproduce thermal load during off-peak hours, and store it for use during peak consumption. Implementations of thermal storage within the context of DG, CHP, and CHCP are quite diverse. Thermal storage cannot produce electrical or thermal load without integration of a suitable powerplant, therefore it is not directly comparable with other systems discussed
in Section 1.4. Thermal storage is a proven option for providing cooling or heating load, and for augmenting the performance of DG, CHP, and CHCP powerplants; it will be briefly discussed as such systems are in use around the world as part of distributed thermal systems. Some implementations of thermal storage include below ground reservoirs (Figure 1-13), integrated reservoirs (Figure 1-14), and two-phase storage [1.14]. There are two main strategies used when implementing thermal storage.

One takes advantage of the large heat capacity, and relatively constant temperature of large underground water reservoirs to provide heating and cooling. It typically takes advantage of a heat pump to extract or reject heat from the reservoir. This method can only be used where large underground reservoirs
of water exist, severely limiting the regions in which such a system can be implemented. Such systems consume electrical power instead of producing it; therefore can only be considered in competition with CHP and CHCP systems when combined with grid power. Two-phase storage is similar to underground storage in that it makes use of the large heat capacity contained in a reservoir of water and ice; the use of two-phase storage increases the specific cooling capacity of underground storage. Large reservoir systems are often used as peaking cycles to reduce electricity consumption during peak hours.

Another interesting implementation of thermal storage comes in the form of inlet cooling for gas turbines. The thermal storage system itself can take the form of
integrated, underground, or two-phase design. However, the cooling product is used to increase specific work output and thermal efficiency of a gas turbine instead of producing cooling load. Estimates place the cost of such a system at 160 USD/kWt of cooling [1.21]. Inlet cooling would benefit a small-scale microturbine-powered trigeneration system, however as a microturbine package can be produced for only 500 to 600 USD/kWe (see Table 1-5), any reduction in specific fuel consumption would have to be weighed against increased specific capital and maintenance costs.

1.5. Thesis objective

The goal of this thesis is to design a trigeneration system targeted for the residential, small business, and institution sectors. This system will be able to be connected to the grid or function as a total energy-islanding device. The system is designed to be in direct economic competition with individual generation from an air conditioning system, natural gas furnace, and grid power. The final design will satisfy the following requirements:

- Be comprised of components that make use of existing technology
- Operation of the system requires no special training, nor should the system require special monitoring.
- Will make use of hydraulic storage combined with an inverse Brayton cycle powered by a microturbine. These technologies will be discussed further in the following section.
• Be sized to provide for all electrical, cooling, and heating loads for a typical detached single family Canadian household.

• The system must not introduce operational health hazards.

• No storage batteries are to be used in the design.

The work contained in this thesis represents the first phase in the design and manufacture of a small-scale trigeneration system. A proof of concept will be built at a later time, as the scope of this thesis is limited to simulation and modelling. Keeping capital costs low will be a priority. Significant emphasis will be placed on maintaining system simplicity, and using low cost components.
Chapter 2
CHCP literature review

2.1. The motivation behind developing CHCP

Technology used in modern CHCP has been available for many years; current efforts are focused on building cycles with proven technology in a fashion that makes economic and thermodynamic sense. The threat of energy shortages, real or imagined, in many places around the world have led many consumers and energy providers alike to look for ways to stretch resources. Trigeneration is seen as one tool to help the new reality facing consumers and energy providers alike.

A key motivation behind trigeneration is to add value to distributed energy systems. Many studies and simulations have shown lower specific capital costs for trigeneration systems over individual generation, in addition to lower specific fuel consumption [2.13]. In some applications where CHP does not make economic sense, the added value of an additional energy product to a CHP system may be more economically viable. By providing cooling output, a trigeneration system enables a building or plant to become completely self-sufficient. This may not be an issue for most, however for total or partial energy islanding, trigeneration packages are very attractive.
2.2. Historical application of CHCP

Historically CHCP has been primarily targeted for use in large institutions and commercial space [2.36]. There are examples of successful CHCP implementation in industry [2.5], however the number of industrial processes that require significant cooling and heating loads are far fewer than those which require one or the other. CHCP has been employed primarily in institutions and commercial buildings due to the agreeable match between building energy product requirements and CHCP energy outputs. Commercial CHCP is a new technology, as the oldest installations are only 8 to 10 years old [2.21] with the majority being only 3 to 4 years old [2.3][2.27][2.31][2.2][2.1]. Over the past decade CHCP systems have achieved economic success while installed in applications such as airports [2.1], shopping centres [2.2], supermarkets [2.21], hospitals [2.36], and industrial plants [2.5][2.3]. The success of existing CHCP plants around the world have motivated Saudi Arabia to form the National Trigeneration CHP Company (NTCC), a government-backed company charged with the development and installation of trigeneration packages throughout the country. With social and environmental responsibility taking a more prominent role around the world, the attractive combination of reductions in energy consumption and carbon emissions is giving trigeneration systems some much needed momentum [2.31]. This momentum is anticipated to give current experimental CHCP systems the opportunity to compete commercially, and to
improve trigeneration technology as a whole via increased competition.

2.2.1. Typical cycle profile of current commercial CHCP

Cycle design for CHCP systems was briefly described in Section 1.1. The following is a more in-depth summary of CHCP systems currently in operation around the world. The most popular choice for trigeneration powerplants are either diesel or gas turbine engines, gasoline internal combustion engines are used on a smaller scale. A typical unit will be in the 3 to 10 MWe output range, which coincides with requirements consistent with large institutions, airports, and hospitals.

Figure 2-1 illustrates three common layouts used for large (3 to 10 MWe) trigeneration systems that incorporate ACR units. Layouts A and B incorporate an internal combustion engine (diesel or gasoline), while layout C uses a gas turbine. The main difference between diesels and gas turbines is the way heat is extracted. When using an internal combustion engine, a significant portion of the waste heat from is in the form of liquid coolant. Layout A provides for one ACR unit by re-circulating the coolant through the exhaust stack, while layout B provides for two ACR units by incorporating exhaust heat into one cycle and coolant flow into the other. Layout B is particularly advantageous for applications that require different temperatures of cooling flow; two ACR units can produce cooling load at two different temperatures. In layout C exhaust circulates directly
through the ACR unit rather than producing steam. This is done to reduce capital and maintenance costs, however an increased pressure drop penalty is paid through the ACR unit.

Figure 2-1: Typical layout for commercial CHCP utilizing diesel or GT powerplants [2.8]
For commercial systems that make use of vapour compression refrigeration units (VCR), there are two primary configurations used: direct drive and indirect drive. The most significant difference between them is how the compressor of the VCR unit is driven. In a direct configuration, a clutched shaft connects the prime mover and the VCR compressor. The VCR unit is engaged by disengaging the clutch, thereby providing direct shaft power to the refrigerant compressor. Conversely, an indirect configuration does not have a direct shaft connection between the prime mover and the VCR compressor. Electrical load is supplied by the generator (which is connected to the prime mover via a shaft), which is used to power the refrigerant compressor.

2.2.1.1. Suitability of VCR and ACR refrigeration for small-scale CHCP

Figure 2-2 is a schematic of an ACR chiller. The chilling effect is produced from energy provided to the generator by high-temperature powerplant exhaust. This system is well suited for CHCP systems as when a heating load is no longer needed or is throttled, exhaust can be re-directed into the ACR rather than dumped overboard, while a VCR CHCP system (see Figure 1-2) does not make use of exhaust heat when producing a cooling load. If heating and cooling loads are required simultaneously (as in the case of a supermarket or food processing plant [2.21]), the VCR-based CHCP system may be a viable option. Since VCR units do not use waste exhaust to provide a cooling effect, they can only remain
competitive with ACR CHCP if exhaust is used for another application such as process heat. Commercial or residential applications have thermal load profiles that are different than typical industrial demands, as heating and cooling loads are not required simultaneously. Despite high coefficient of performance (COP) values for VCR systems (high-performance VCR residential air conditioners demonstrate COP values of about 3 or more [2.16]), VCR CHCP systems can only economically operate with applications that require simultaneous cooling and heating loads. This is due to the fact that exhaust heat is not utilized in summer months when only cooling and electrical loads are required.

Figure 2-2: Schematic of a double-effect LiBr absorption chiller adapted from [2.9]
To maintain high overall efficiency without having to produce both cooling and heating loads simultaneously, ACR refrigeration based CHCP is a more suitable choice. Another factor leading to the domination of ACR over VCR in the trigeneration market is the fact that electrical load is more economically valuable than thermal output. Electrical load can either be used to satisfy electrical loads that would have been purchased, or can be sold back to the grid to generate income. Unlike electrical load waste heat cannot be exported for profit, and is cheaper to produce; hence using electrical load to power a VCR as part of CHCP system unit is not often an economical choice. There are two predominant ACR configurations used in CHCP systems today: single-effect and double-effect ACR. The single-effect ACR uses only exhaust heat to evaporate the working fluid, while the double-effect includes an additional fired generator seen in Figure 2-2. Double-effect ACR can double the COP of single-effect ACR, but also has 20 to 70 percent higher specific capital and maintenance costs [2.23]. As is shown in Figure 2-2, an ACR unit is complex requiring many expensive components in addition to a cooling tower not shown in the diagram. The capital cost for ACR units rises dramatically for smaller units and becomes prohibitively expensive for units sized for a typical household (about 10 to 11 kWt).

Figure 2-3 contains ACR specific capital costs from several suppliers, and provides a curve fit for small and large-scale chillers. Using the curve fit for small
chillers (Equation (2-1)) [2.11], an ACR unit sized for a single family detached household would cost about 6400 USD to purchase and install; this cost does not include purchase and installation of a cooling tower; add to this yearly maintenance costs of about 250 USD (see Figure 2-4) for the ACR unit alone.

\[
\frac{USD}{kWt} = -81.552 \ln(kWt) + 778.95
\]  

\[\text{(2-1)}\]

Figure 2-3: Specific capital costs for absorption chillers with curve fits for large and small-scale chillers [2.11]

These costs prevent ACR technology from being considered for small-scale
trigeneration as in addition to an expensive chiller and cooling tower, a
trigeneration system requires the purchase of at least a powerplant in addition to
other auxiliary systems. It is clear that an economically successful small-scale
CHCP system cannot use ACR or VCR chilling units in order to compete with
individual generation system (natural gas furnace, VCR chiller, and grid power)
as is common for many North American residential or small-scale commercial
applications.

![Graph showing specific maintenance costs for absorption chillers](image)

**Figure 2-4: Specific maintenance costs for absorption chillers [2.11]**
2.2.2. Production CHCP packages

Current CHCP packages are most commonly designed using off-the-shelf individual components that are matched together in an ad hoc genset package. There are many companies making attempts at proving CHCP technologies in conjunction with the US Department of Energy, however these CHCP installations are not packaged units [2.10]. They are highly experimental and custom built, involving a high degree of design overhead.

At this time, UTC Power is the only company breaking this tradition by offering the first packaged trigeneration system on the market. This package uses four Capstone microturbines and a LiBr absorption chiller to provide: 227 kWe, 500 kWt cooling load, and 70 kWt heating load at 91 percent overall efficiency when operating in cooling mode. The system can also provide 227 kWe and 322.3 kWt at 68 percent overall efficiency in heating mode [2.28]. UTC Power boasts a 46 percent reduction in CO₂ emissions over coal-fired grid power and an average cost savings of 10,000 USD monthly. The system is currently installed in hotels, supermarkets, and shopping centres around the United States.

2.3. Experimental small-scale CHCP systems

The main focus of experimental CHCP research is centred on small-scale applications. Perhaps this is due to the fact that large-scale CHCP systems are
more established, and have demonstrated success in the marketplace while small-scale systems have not. Experimental small-scale CHCP systems published in open literature typically use an internal combustion engine (ICE) as the cycle powerplant as seen in Table 2-1. Examples of the experimental apparatuses can be found in Appendix A. Variation in size of the systems described in Table 2-1 illustrates the scalable nature of small-scale CHCP. The above systems were subjected to loading schemes consistent with an average household and analysed in terms of thermodynamics and economics. All three systems offered improvements in primary energy use when compared to individual generation; experimental data indicates a conservative value of 23 percent is realistically obtainable in practice [2.17].

Table 2-1: Performance data for several experimental small-scale CHCP systems at ISO conditions

<table>
<thead>
<tr>
<th>Prime Mover</th>
<th>Refrigeration method</th>
<th>Total Efficiency</th>
<th>Electrical Output (kW)</th>
<th>Heating Output (kW)</th>
<th>Cooling Output (kW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gasoline ICE [2.15]</td>
<td>ACR</td>
<td>70</td>
<td>12</td>
<td>27</td>
<td>9</td>
</tr>
<tr>
<td>Gasoline ICE [2.24][2.25]</td>
<td>VCR</td>
<td>58-65*</td>
<td>1.5</td>
<td>19.6</td>
<td>9.1</td>
</tr>
<tr>
<td>Natural gas ICE [2.12]</td>
<td>Ejector**</td>
<td>50</td>
<td>5.34</td>
<td>5</td>
<td>1</td>
</tr>
</tbody>
</table>

* values for ISO standard atmosphere not given, data taken for cooling production during summer months
** a brief description of the ejector cooling cycle can be found in Appendix F

These systems are comprised completely from off-the-shelf components, however there is substantial variation in performance data. Overall thermal
efficiency varies from 70 to 90 percent when producing cooling load, and primary energy reduction over individual generation varies between 23 to 66 percent. The largest differences between the apparatuses in question can be found in the cooling subsystems used. Due to the low COP of ACR units (0.6 to 1.2) [2.8][2.15][2.28], the efficiency of CHCP systems typically is larger during a heating or power mode. For the system using an ACR unit in Table 2-1, the overall efficiency varies between 70 to 75 percent when switching from cooling to heating modes. This variation may seem substantial, but is minor when compared to the reduction in overall efficiency experienced by CHCP systems utilizing VCR units during cooling only modes of operation.

The efficiencies quoted in Table 2-1 were obtained assuming all the energy products are utilized. For example, the ICE-ACR system produces adequate levels of cooling and heating load to meet a typical household demand of 1 to 4 kWt and 6 to 14 kWt respectively (see Section 3.4.3), but overproduces electrical load. Unless this load can be sold back to the grid, overproduction is a penalty on efficiency. Even if this load can be sold back to the grid, power utilities often charge connection fees and purchase power at a significantly reduced rate that may not compensate adequately for the actual cost of production. Conversely, the ICE-ejector system produces an adequate level of electrical load but severely under produces thermal loads. Within the context of a small-scale non-industrial
process where loads vary widely, experimental small-scale CHCP systems currently discussed in open literature require additional components to buffer loads. This can take the form of a battery system to deal with over- or under-production of electrical load, or a backup boiler or furnace to deal with peak thermal loads. The systems shown in Table 2-1 are insufficient to replace individual generation systems while maintaining or improving economic performance.

All three systems were compared to individual generation of electrical and thermal loads on site. System economic performance was not compared against purchasing grid power, electric load was satisfied on site with a generator. This is not a fair economic comparison, as most consumers regardless of size or classification (commercial, industrial, residential) do not generate power on site. Designing CHCP systems that are economically superior to grid power is much more difficult to accomplish, as grid power is usually significantly cheaper to purchase than it is to produce using a genset; the system described in Chapter 3 is designed to compete with grid power.

2.4. Simulated small-scale CHCP systems

In addition to experimental small-scale CHCP systems discussed in open literature, there are several simulated systems that warrant comment. Two
systems in the sub 100 kWe range were found, summarized in Table 2-2.

Table 2-2: Performance data for simulated small-scale CHCP systems

<table>
<thead>
<tr>
<th>Prime Mover</th>
<th>Cooling method</th>
<th>Overall Efficiency</th>
<th>Electrical Output (kW)</th>
<th>Heating Output (kW)</th>
<th>Cooling Output (kW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Microturbine [2.17]</td>
<td>ACR and VCR</td>
<td>70</td>
<td>100</td>
<td>117.6</td>
<td>75.8</td>
</tr>
<tr>
<td>Stirling [2.14]</td>
<td>ACR</td>
<td>89</td>
<td>50</td>
<td>76</td>
<td>70</td>
</tr>
</tbody>
</table>

The microturbine powered CHCP simulation ran two iterations which differed in the method by which thermal load was provided; one used an ACR unit, while the other used a heat exchanger and VCR unit. A load profile based upon a commercial retail space was used, the dimensions of the space was scaled according to the thermal output of the CHCP system. As was expected, the ACR unit was superior to the VCR unit economically based upon a full year simulation; capital costs were not taken into account in the simulation. Similar to the experimental systems, both simulated systems made the key assumption that all energy products were used on site in overall efficiency and economic calculations, which is most likely not the case.
2.5. Hydraulic storage and the inverse Brayton cycle

Hydraulic storage has been used for a variety of purposes; this includes providing power for shop tools and industrial machinery, providing pneumatic power for assembly line automation, and for providing propulsion via hydraulically powered motors as early as 1879 [2.4] [2.19]. The idea of using compressed air storage as energy storage (CAES) for power generation was first investigated by the General Electric Company and the Brown Boveri Company (later renamed ABB) in the mid 1970s [2.33] [2.35]. Compressed air was stored in an underground cavern during off-peak hours. During peak hours when load exceeds nominal generation capacity, the high-pressure cavern air is passed through a combustion chamber and then into an expander to provide electrical load. Several independent studies have compared the capital and operational costs of the cavern-CAES system to a gas turbine plant of equal electrical output, and have concluded the cavern-CAES system demonstrates lower operational costs without significantly higher capital investment costs [2.33][2.26][2.30][2.29]. The cavern-style system is tailored for large MW scale power producers, the economic success of which has motivated smaller spin-off technologies.

Active Power, a company based in Austin, Texas has used compressed air storage with an expansion turbine to provide short-term backup power [2.30]. This system is designed to replace battery based UPS systems for servers and
other sensitive equipment and is capable of providing 20 kWe of continuous power for 15 minutes. Some key advantages of the system include a long service life of 20 years, a higher power density than lead acid batteries, and modular construction. There is no danger of power discharge during storage, ensuring 100 percent readiness at all times. This system demonstrates the environmental benefits of using CAES. Eliminating space consuming, environmentally harmful batteries, which require frequent replacement not only improves system life, but is also more suited to a growing population of consumers who wish to reduce their environmental impact.

Others have seen the potential for small-scale hydraulic storage power systems and have attempted to improve on the idea. A team from Lausanne, Switzerland has modelled and built an experimental prototype of a hydraulic-pneumatic storage hybrid system that promises greater efficiency and energy density over a strictly pneumatic system [2.29]. The system uses a motor/generator to pump hydraulic fluid into an accumulator already pressurized with air. When emergency power is required, high-pressure hydraulic fluid is discharged through a hydraulic motor, producing 1 to 4 kWe via the motor/generator. This system has the advantage of extracting work from the hydraulic fluid at higher efficiencies than a turbo-expander can from air; using a liquid as the working fluid allows much higher specific work output as well. The end result is a significantly higher power
density when compared to the compressed air UPS system. Both of the described systems are useful for their intended purposes, but are strictly limited to very short periods of discharge. In an effort to extend the concept of the IBC to a continuous flow process, several alternative applications have been developed.

![Figure 2-5: Schematic of an IBC refrigeration system designed for use in road transport applications [2.32]](image)

IBC refrigeration is popular with transportation industries such as aviation and rail for space cooling [2.7]. Since IBC refrigeration uses air as the working fluid, the need for liquid refrigerants, associated storage tanks, high-pressure lines, and compressors are eliminated. It has even been suggested that IBC refrigeration could be useful for road transport as well, seen in Figure 2-5 [2.32]. In a world of increasingly tighter environmental requirements, a refrigeration system that does not require controlled substances such as a refrigerant is very appealing.
In general, IBC refrigeration cycles demonstrate COP values half that of VCR units if generic components are used. However IBC refrigeration COP approaching or exceeding that of VCR units has been demonstrated for optimized systems built using specifically designed turbomachinery and heat exchanging equipment [2.7][2.32]; this emphasises the importance of careful design of an IBC system. Inefficient designs could result in unnecessary abandonment due to poor performance results.

IBC technologies can be applied to gensets as well. Gas turbines experience significant reductions in specific power output and thermal efficiency in high-temperature environments. Systems have been proposed to reduce inlet temperatures including thermal storage [2.20], evaporative cooling [2.6], and IBC refrigeration [2.34]. Gas turbines have very high mass flow rates when compared to reciprocating engines, and therefore require high-capacity inlet cooling refrigeration equipment; IBC refrigeration systems have similar mass flow rates to gas turbines, making them ideal for increasing performance of gas turbine gensets in hot weather conditions.
A research consortium headed by Building Research Consultants (BRC) based in the UK is investigating the feasibility of the IBC concept for building heating and cooling [2.7]. The simulated system is designed to provide a simultaneous 80 kWt cool water load and 20 kWt hot water load. The refrigeration side demonstrated COP values of about 0.6, which is equivalent with single-effect absorption chillers [2.9] while the heating side demonstrated COP values of 1.5. Despite having low refrigeration COP values when compared to modern VCR units, performance was found to be invariant with respect to outside air...
temperature. It is anticipated that over a full year the IBC system can remain competitive with heat pumps and VCR units, which will be investigated with experimentation.

2.6. Summary

CHCP systems are relatively new, having been used in commercial and industrial installations only within the past 10 to 15 years. Historically, CHCP systems have been targeted for large industrial or commercial processes where electrical and thermal loads are relatively constant. This permits a CHCP system to be sized such that at full capacity there is no over-production of thermal or electrical loads; small-scale applications of CHCP technology require more flexibility as load profiles are highly variable.

While there is evidence of research and development in the area of small-scale CHCP technology, the majority of commercial development is in the greater than 100 kWe range. This can be attributed to increasing specific capital costs as CHCP systems are decreased in size; primarily due to the high cost of absorption chillers, the most popular method of providing a thermal load in a CHCP system.

CHCP systems are still only available commercially as custom-built packages from a select few companies; currently United Technologies is the only company offering a standardized CHCP package. Experimental and simulated systems are
discussed in open literature, however they are often sized for medium to large applications (greater than 50 kWe). There is no system currently discussed in open literature, or available on the market, that provides an energy islanding CHCP solution for residential or small-scale commercial users at an economical specific capital and maintenance cost.

While CHCP systems may be relatively new, the use of accumulators in combination with the IBC is not. The two concepts have been combined to produce emergency power, but have not been applied to a continuous flow power cycle for small-scale application before. The IBC has been used for mobile refrigeration applications, and more recently is being applied to building heating and cooling. Despite the wide variety of simulated, tested, and commercially applied IBC systems, there exists no IBC system applied to a trigeneration cycle for small-scale applications. This thesis will investigate the feasibility of such a system and report on simulated thermodynamic and economic performance. The simulated trigeneration system will be compared against individual generation using an air conditioning system, natural gas furnace, and grid power.
Chapter 3
Description of Model and Simulation

3.1. Overview of Model
This section describes the design and simulation of an indirectly fired trigeneration system with hydraulic accumulation as shown in Figure 3-2 and Figure 3-3. The system is composed of a conventional microturbine, with a network of heat exchangers in lieu of a conventional burner section. By using an indirectly fired process, combustion gases never mix with microturbine flow, allowing microturbine exhaust to be used for household heating or cooling. An air accumulator is used as an energy storage device when the microturbine overproduces electrical load. The compressed air stored in the accumulator is used to generate power and thermal loads when the microturbine is turned off. Two different heat exchanger configurations are used, Mode 1 for heating loads, and Mode 2 for cooling loads as shown in Figure 3-2 and Figure 3-3 respectively.

3.2. Initial system design
The initial concept for the trigeneration system had one configuration for cooling and heating modes as shown in Figure 3-1. Key differences between the initial concept and the final system shown in Figure 3-2 and Figure 3-3 are summarized here:

- Initial system design called for the accumulator to be charged with bleed air
from the microturbine compressor instead of using a separate compressor

- Same HEN configuration was used for both cooling and heating modes
- No secondary expander
- No in-ground #4 Hx
- Accumulator flow was not cycled through the HEN in heating mode

Once initial simulations were run, it was immediately apparent that the initial configuration had operational difficulties that would prevent it from satisfying a highly variable thermal and electrical load. The following sections describe the modifications made to the base system in an effort to increase thermodynamic and economic performance, and the related effect on system response.
Figure 3-1: Original trigeneration system design
3.3. Final system design

The following is a description of the final configuration and method of operation used in the final simulation.

MICROTURBINE OPERATION:

In this system, the microturbine is used to:

1) Meet household electrical load demands.

2) Provide a heat load when operating in Mode 1.

3) Charge the accumulator.

As the microturbine almost always produces an electrical output in excess of household demand, the excess is fed to a secondary compressor which charges the accumulator.

INVERSE BRAYTON CYCLE (IBC):

The IBC is used to:

1) Provide household electrical load when the microturbine is not running.

2) Provide a heating load in Mode 1 when the microturbine is not running.

While the microturbine produces a thermal load in excess of household demand, the IBC produces less than household demand.

3) Meet household cooling load in Mode 2. The IBC consists of the secondary compressor, #4 Hx, accumulator, and secondary expander.
GENERAL ASSUMPTIONS AND CONSTANTS:

The following are a set of assumptions and constants that are applied to all components and throughout the simulation:

- Air was treated as a perfect gas with a composition of 21 percent O₂, 79 percent N₂, and zero moisture
- No transient behaviour was modelled
- \( P_a = 101.325 \text{ kPa} \)
- \( R = 287 \text{ J/kgK} \)

MODE 1:

Is used to produce electric and heat loads. Mode 1 does not cycle microturbine expander exhaust through the heat exchanger network (HEN), thereby providing high temperature flow for household heating. During accumulator discharge, accumulator flow is directed through the HEN where flow temperature is increased before discharge through the secondary expander; this increases the thermal output of the IBC.

MODE 2:

Is used to produce a cooling load. Microturbine exhaust is no longer required for heating purposes, therefore it is used to pre-heat HEN combustion air before being vented to atmosphere. Mode 2 meets household thermal demands using
the IBC alone, instead of a combination of microturbine and IBC as does mode 1.

In order to meet a cooling load, secondary compressor discharge flow is cooled using #4 Hx before passing into the accumulator. This ensures the air in the accumulator is at or below ambient, for use in cooling load production. During accumulator discharge, expansion through the secondary expander produces electrical power and low temperature exhaust suitable for household cooling.

As there are a number of components that require modelling, for ease of understanding this section is broken into five sub-groups: 1) the HEN 2) microturbine 3) secondary turbomachinery 4) accumulator 5) the individual generation system.
Figure 3-2: Schematic of trigeneration system in heating mode (Mode 1)
Figure 3-3: Schematic of trigeneration system in cooling mode (Mode 2)
Figure 3-4: T-s diagram for the IBC in heating mode. Dashed lines represent the ideal cycle without pressure losses and isentropic expansion and compression processes. The solid line is the actual cycle which takes into pressure losses, isentropic efficiencies, and losses when discharging to the accumulator.

While the combination of the microturbine and HEN produce a standard Brayton cycle T-s diagram for both heating and cooling modes, the IBC has a slightly different diagram for each mode shown in Figure 3-4 and Figure 3-5. As secondary compressor flow is discharged to the accumulator, the flow will expand to accumulator pressure. For the ideal cycle in both heating and cooling modes, this process will generate less entropy than the actual case, as is shown
in Figure 3-4 and Figure 3-5. The actual case also takes into account pressure losses in the HEN and exhaust ducting of the microturbine.

Figure 3-5: T-s diagram for the IBC in cooling mode. Dashed lines represent the ideal cycle without pressure losses and isentropic expansion and compression processes. The solid line is the actual cycle which takes into pressure losses, isentropic efficiencies, and losses when discharging to the accumulator.

While the impact of the zero moisture assumption on system performance is unknown (the presence of moisture will increase the specific work output of the microturbine, however the exact impact on thermal efficiency is unknown),
operational impact is less ambiguous. The presence of micro droplets in the air poses a problem for turbomachinery, as impingement of these droplets will have a negative impact on efficiency and cause pitting on blade and stator surfaces. Presence of moisture in the IBC flow path will pose a problem for accumulator and valve oxidation, in addition to the impact on turbomachinery. Drying inlet air is a prudent course of action, should the theoretical model described in this chapter be practically implemented.

3.3.1. Heat exchanger network (HEN)

The HEN is required to indirectly fire the microturbine. A series of three heat exchangers are used to raise the temperature of compressor discharge flow before discharge to the microturbine expander. The HEN operates in two different configurations for heating and cooling loads, and are described separately. This section deals with both on-design and off-design operation of the HEN.

3.3.1.1. On-design operation (maximum #2 Hx temperature operation)

ASSUMPTIONS AND CONSTANTS:

- $\varepsilon = 0.9$ for all exchangers
- Zero fouling was assumed
- $\Delta P_{hx} = 2$ percent (applied across each heat exchanger)
• $\eta_{comb} = 0.99$

• Combustion side and air side mass flows are equal

• $T_{max} = 1200$ K

• Ground around #4 Hx has an infinite heat capacity and a constant temperature of 8°C (281 K)

• Fuelled with natural gas (LHV = 50 MJ/kg)

INPUTS:

• Compressor discharge enthalpy and pressure: $h_{12}, P_{12}$

• Ambient conditions: $h_a, P_a$

OUTPUTS:

• Specific fuel flow: $\dot{m}_f$

• Expander inlet enthalpy and pressure: $h_{14}, P_{14}$

DECISION CHARTS:
THEORY:

Equations for heat exchanger effectiveness (Equation (3-1)) and the 1st law of thermodynamics (Equation (3-2)) were applied to each exchanger in the network. With respect to Equations (3-1) and (3-2), the subscripts C and H stand for cold and hot streams respectively.

\[
\varepsilon = \frac{h_{C,\text{out}} - h_{C,\text{in}}}{h_{H,\text{in}} - h_{C,\text{in}}} \quad (3-1)
\]

\[
\dot{m}_C (h_{C,\text{out}} - h_{C,\text{in}}) = \dot{m}_H (h_{H,\text{in}} - h_{H,\text{out}}) \quad (3-2)
\]

Using Mode 1 as an example, the following six equations result from the
application of Equations (3-1) and (3-2) to the HEN:

\[ \varepsilon = \frac{h_{13} - h_{12}}{h_{24} - h_{12}} \]  
(3-3)

\[ \varepsilon = \frac{h_{14} - h_{13}}{h_{23} - h_{13}} \]  
(3-4)

\[ \varepsilon = \frac{h_{22} - h_{21}}{h_{25} - h_{21}} \]  
(3-5)

\[ h_{13} - h_{12} = h_{24} - h_{25} \]  
(3-6)

\[ h_{14} - h_{13} = h_{23} - h_{24} \]  
(3-7)

\[ h_{22} - h_{21} = h_{25} - h_{26} \]  
(3-8)

Equations (3-3) through (3-8) are then manipulated into an Ax=b format by placing all unknown variables on the left hand side and all known variables on the right hand side of the equation:

\[
\begin{bmatrix}
0 & 0 & -1 & 0 & \varepsilon & 0 \\
-1 & 0 & 0 & \varepsilon & 0 & 0 \\
1 - \varepsilon & -1 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & -1 & 1 \\
1 & 0 & 0 & -1 & 1 & 0 \\
-1 & 1 & 0 & 1 & 0 & 0
\end{bmatrix}
\begin{bmatrix}
h_{13} \\
h_{14} \\
h_{22} \\
h_{24} \\
h_{25} \\
h_{26}
\end{bmatrix}
= \begin{bmatrix}
(\varepsilon - 1)h_{21} \\
(\varepsilon - 1)h_{12} \\
-\varepsilon h_{23} \\
h_{21} \\
h_{12} \\
h_{23}
\end{bmatrix}
\]  
(3-9)

After solving Equation (3-9) by inverting the solution matrix, specific fuel flow can be calculated using the following:
HEN discharge pressure (expander inlet pressure) is calculated using the assumption that each heat exchanger has a 2 percent pressure loss:

\[ P_{14} = P_{12} \left( 0.98^2 \right) \]  

Heat exchanger #4 is not included in the HEN system of equations as there is no relationship between the inlet and outlet enthalpies of the #4 Hx and the HEN. The inlet and outlet enthalpies of the HEN are not independent of one another; they must be solved simultaneously. This is not true for #4 Hx, which is independent of the HEN. The discharge temperature for #4 Hx is simply calculated using an adaptation of Equation (3-1) where \( T_{\text{out}} \) is accumulator inlet temperature and \( T_{\text{in}} \) is secondary compressor discharge temperature; an effectiveness of 0.95 was assumed for the #4 Hx:

\[ T_{\text{out}} = \varepsilon_4 \left( T_{\text{ground}} - T_{\text{in}} \right) + T_{\text{in}} \]  

The HEN solution method for Mode 2 differs from Mode 1. This is due to the fact that as flow is directed through different paths from the heating mode, there are different unknowns. The cooling mode system of equations has one more unknown than equations. It therefore has to be implicitly solved with expander discharge temperature Equations (3-26) and (3-27). This is done by using a symbolic variable for \( h_{15} \) to allow MATLAB™ to solve the system of equations.
symbolically, instead of in a closed equation format as was done for the heating mode. The system of equations for Mode 2 is as follows:

\[ \epsilon_1 = \frac{h_{13} - h_{12}}{h_{24} - h_{12}} \] (3-13)

\[ \epsilon_2 = \frac{h_{14} - h_{13}}{h_{23} - h_{13}} \] (3-14)

\[ \epsilon_3 = \frac{h_{22} - h_{21}}{h_{15} - h_{21}} \] (3-15)

\[ h_{13} - h_{12} = h_{24} - h_{25} \] (3-16)

\[ h_{14} - h_{13} = h_{23} - h_{24} \] (3-17)

\[ h_{22} - h_{21} = h_{15} - h_{16} \] (3-18)

\[
\begin{bmatrix}
1 - \epsilon & -1 & 0 & 0 & 0 & 0 \\
-1 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & -1 & 0 & 0 \\
1 & 0 & 0 & 0 & -1 & 1 \\
-1 & 1 & 0 & 0 & 1 & 0 \\
0 & 0 & 1 & 1 & 0 & 0
\end{bmatrix}
\begin{bmatrix}
h_{13} \\
h_{14} \\
h_{15} \\
h_{16} \\
h_{22} \\
h_{25}
\end{bmatrix}
= 
\begin{bmatrix}
-h_{25} \epsilon \\
h_{12} / (\epsilon - 1) \\
h_{21} (\epsilon - 1) - h_{15} \epsilon \\
h_{12} \\
h_{23} \\
h_{21} + h_{15}
\end{bmatrix}
\] (3-19)

As was mentioned previously, Equation (3-19) is solved in terms of \( h_{15} \); \( h_{14} \) is therefore as a function of the as of yet unknown \( h_{15} \). Equations (3-26) and (3-27) require \( h_{14} \) to be converted into \( T_{14} \). However as \( h_{14} \) is expressed in terms of \( h_{15} \), the system of equations generated must be solved simultaneously.
and implicitly. Air-side flow passes through one more heat exchanger (#3 Hx) in Mode 2, therefore HEN discharge pressure is calculated using Equation (3-20):

\[ P_{14} = P_{12} \left(0.98^3\right) \]  

(3-20)

3.3.1.2. Off-design operation (EIT specified)

To reduce the output power of the microturbine, the EIT must be reduced. As such off-design operation needs to be taken into consideration. Equations (3-9) and (3-19) cannot be used for off-design operation, as \( T_{\text{max}} \) (and by extension \( h_{23} \)) becomes an unknown and must be removed from the solution matrix. \( T_{14} \) (EIT) is specified in off-design operation, therefore has to be removed from the unknowns vector and put into the solution matrix. The inputs, assumptions, and constants remain unchanged from on-design operation and can be found in Section 3.3.1.1. Equations for HEN discharge pressure \( (P_{14}) \) also remain unchanged.

OUTPUTS:

- Specific fuel flow: \( \dot{m}_f \)
- Expander inlet pressure: \( P_{14} \)
- HEN maximum temperature: \( T_{23}, h_{23} \)
DEcision Charts:

Figure 3-8: Mode 1 off-design decision chart.

Figure 3-9: Mode 2 off-design decision chart.

Theory:

The system of equations remains unchanged from on-design operation for both Mode 1 and 2, however the variables are separated differently to account for the change in known and unknown variables. The system of equations for Mode 1 in off-design is shown in Equation (3-21):
The HEN solution matrix for Mode 2 off-design operation is slightly different from Mode 1 off-design because it includes the expander discharge enthalpy \( h_{15} \). It is possible to calculate this value without first solving the HEN solution matrix, as in off-design expander inlet temperature is specified. Unlike on-design operation, the Mode 2 off-design system of equations does not need to be solved implicitly using root finding methods. The corresponding system of equations for off-design Mode 2 is found in Equation (3-22):

\[
\begin{bmatrix}
1 - \varepsilon & \varepsilon & 0 & 0 & 0 & 0 \\
-1 & 0 & 0 & 0 & \varepsilon & 0 \\
0 & 0 & 0 & -1 & 0 & 0 \\
1 & 0 & 0 & 0 & -1 & 1 \\
-1 & -1 & 0 & 0 & 1 & 0 \\
0 & 0 & 1 & 1 & 0 & 0
\end{bmatrix}
\begin{bmatrix}
h_{13} \\ h_{23} \\ h_{16} \\ h_{22} \\ h_{24} \\ h_{25}
\end{bmatrix}
= 
\begin{bmatrix}
h_{14} \\ h_{12} (\varepsilon - 1) \\ h_{21} (\varepsilon - 1) - h_{15} \varepsilon \\ h_{12} \\ -h_{14} \\ h_{21} + h_{15}
\end{bmatrix}
\tag{3-22}
\]

The governing equation for the \#4 Hx does not change for on- or off-design operation, and can be found in the previous section (Equation (3-12)).
3.3.2. Microturbine

The microturbine is comprised of two components: the compressor and expander. While the equations used for each component are identical in form, the station numbering is different. To avoid confusion, each component will be treated separately.

3.3.2.1. Microturbine compressor

ASSUMPTIONS AND CONSTANTS:

- $\eta_c = 0.75$ at design for ISO standard atmospheric conditions
- CPR = 4 at design for ISO standard atmospheric conditions
- No microturbine compressor overboard bleed or expander cooling flows
- No inlet pressure losses

INPUTS:

- Ambient temperature and pressure: $T_a, P_a$

OUTPUTS:

- Compressor discharge temperature and pressure: $T_{12}(h_{12}), P_{12}$
DEcision chart:

Figure 3-10: Microturbine compressor decision chart.

Theory:

For the compression process, Equation (3-23) is used to determine the isentropic discharge temperature. Once an isentropic discharge temperature is determined, this is converted to an actual temperature using Equation (3-24) through the use of an isentropic efficiency. A curve fit for $C_p(T)$ is taken from [3.9] for use in Equation (3-23):

$$\int_{T_{11}}^{T_{12}} \frac{C_p(T)}{T} \,dT - R \ln \left( \frac{P_{12}}{P_{11}} \right) = 0$$  \hspace{1cm} (3-23)

$$T_{12} = T_{11} + \frac{T_{11}}{\eta_c} \left( \frac{T_{12s}}{T_{11}} - 1 \right)$$  \hspace{1cm} (3-24)

Compressor discharge pressure is calculated using the following equation:

$$P_{12} = P_a(CPR)$$  \hspace{1cm} (3-25)
3.3.2.2. Microturbine expander

Since the expander is basically the reverse process of the compressor, the theory is similar.

ASSUMPTIONS AND CONSTANTS:

- $\eta_e = 0.84$ at design for ISO standard atmospheric conditions
- Expander discharge pressure is 2 percent above $P_a$
- No cooling flows

INPUTS:

- HEN discharge temperature and pressure: $T_{14}$ ($h_{14}$), $P_{14}$
- Ambient pressure: $P_a$

OUTPUTS:

- Expander discharge temperature and pressure: $T_{15}$ ($h_{15}$), $P_{15}$
**THEORY:**

For the expansion process Equation (3-26) was used to determine the isentropic expander discharge temperature. Equation (3-27) was used to convert to an actual temperature using an isentropic efficiency. A curve fit for $C_p(T)$ was taken from [3.9] for use in Equation (3-26).

$$\int_{T_{14}}^{T_{15s}} \frac{C_p(T)}{T} dT - R \ln \left( \frac{P_{15}}{P_{14}} \right) = 0 \quad (3-26)$$

$$T_{15} = T_{14} + T_{14} \eta_e \left( \frac{T_{15s}}{T_{14}} - 1 \right) \quad (3-27)$$

Expander discharge pressure was calculated using Equation (3-28):

$$P_{15} = 1.02 P_a \quad (3-28)$$

**3.3.2.3. Microturbine performance**

Using the outputs from the compressor, expander, and the HEN, microturbine
performance was calculated.

ASSUMPTIONS AND CONSTANTS:

- $\dot{W} = 10 \text{ kWe at design and ISO standard atmospheric conditions}$
- $\eta_m = 0.96$
- $LHV = 50 \text{ MJ/kg (natural gas)}$

INPUTS:

- Compressor inlet and discharge enthalpy: $h_{11}, h_{12}$
- Expander inlet and discharge enthalpy: $h_{14}, h_{15}$
- Household ambient enthalpy: $h_h$
- HEN specific fuel flow: $\dot{m}_f$

OUTPUTS:

- Microturbine mass flow, heat output, and thermal efficiency: $\dot{m}, \dot{Q}, \eta_{th}$
- HEN fuel flow: $\dot{m}_f$
DECISION CHART:

Figure 3-12: Microturbine performance decision chart.

THEORY:

For a required work output, microturbine mass flow and the HEN fuel flow are calculated:

\[
\dot{m} = \frac{\dot{W} \eta_m}{(h_{14} - h_{15}) - (h_{12} - h_{11})} \tag{3-29}
\]

\[
\dot{m}_f = \dot{m} \dot{m} \tag{3-30}
\]

With microturbine mass flow known, the heat output of the microturbine is calculated as follows:

\[
\dot{Q} = \dot{m} (h_{15} - h_h) \tag{3-31}
\]

Finally, microturbine thermal efficiency is calculated:

\[
\eta_{th} = \frac{\dot{W}}{LHV\dot{m}_f} \tag{3-32}
\]
3.3.2.4. Off-design performance

Off-design microturbine performance was predicted using generic compressor and expander maps incorporated into GASTURB [3.6]. These maps represent an averaging of several actual turbomachinery maps to approximate conventionally designed compressors and expanders used in gas turbines.

ASSUMPTIONS AND CONSTANTS:

- Reference temperature and pressure: $T_{\text{ref}} = 288 \, \text{K}$, $P_{\text{ref}} = 101.325 \, \text{kPa}$

INPUTS:

- Required microturbine power output: $\dot{W}$
- Ambient temperature and pressure: $T_a$, $P_a$

OUTPUTS:

- Microturbine mass flow, heat output, and thermal efficiency: $\dot{m}$, $\dot{Q}$, $\eta_{th}$
- Microturbine fuel flow: $\dot{m}_f$
DEcision Chart:

- Calculate $h_{12}, h_{14}, h_{15}, P_{14}$ using methods described in Sections 3.1.1.1 through 3.1.1.3

- Calculate microturbine EPR

- Get corrected expander mass flow and isen. eff. from curve fit

- Calculate expander mass flow

- Calculate $\dot{W}$

- $T_a, \bar{P}_a, \bar{W}$

- Guess microturbine CPR

- Get corrected compressor mass flow and isen. eff. from curve fit

- Calculate compressor mass flow

- Is calculated $\dot{W}$ close enough to desired $\dot{W}$?

**Figure 3-13: Microturbine off-design decision chart.**

**Theory:**

A constant speed operating line was modelled in GASTURB™ by varying the output power from design to synchronous idle. Corrected compressor mass flow, CPR, EPR, isentropic efficiencies, and corrected expander mass flow were then normalized by design point values to capture trends as shown in Figure 3-14. These normalized values were then multiplied by design point performance predictions from the in-house model to generate a constant speed off-design
The operating line was expressed in the form of four curve fits:

- Corrected compressor mass flow as a function of CPR.
- Compressor isentropic efficiency as a function of CPR.
- Corrected expander mass flow as a function of EPR.
- Expander isentropic efficiency as a function of EPR.
Calculating off-design performance was an iterative process that was broken down into the following steps:

1) For a given ambient temperature and pressure, select a desired work output.

2) Guess a CPR. Calculate corrected compressor mass flow and compressor isentropic efficiency from operating line curve fits.

3) Calculate compressor mass flow using Equation (3-33).

4) Calculate $h_{12}$, $h_{14}$, $h_{15}$, $P_{14}$ using methods described in Sections 3.3.2.1 and 3.3.2.2

5) Calculate EPR and then get corrected expander mass flow and expander isentropic efficiency from operating line curve fits.

6) Calculate expander mass flow using Equation (3-34).

7) Calculate microturbine power output using methods described in Section 3.3.2.3. Compare calculated output with desired output. If difference is within an acceptable tolerance, terminate calculations. If not, make another guess for CPR and continue iterations.

$$
\dot{m}' = \frac{\dot{m} \frac{P_a}{P_{\text{ref}}}}{\sqrt{\frac{T_a}{T_{\text{ref}}}}} \quad (3-33)
$$
3.3.3. Secondary turbomachinery

In addition to the microturbine, there are two other turbomachinery components to model. The secondary compressor draws power from microturbine electrical output to charge the accumulator, and the secondary expander accepts discharge flow from the accumulator to provide household power and thermal loads.

3.3.3.1. Secondary compressor

The secondary compressor was modelled using performance charts from a commercially available screw compressor. Data for the compressor was digitized from which curve fits for mass flow, power input, and isentropic efficiency were calculated without the need for Equation (3-23); Equation (3-24) was used to determine discharge temperature. The second compressor operates at a constant pressure rise of 4 bar in Mode 1 and 6 bar in Mode 2. Isentropic efficiencies vary between 0.60 and 0.92 depending on the mass flow. Digitized performance graphs and isentropic efficiency curves can be found in Appendix E.
ASSUMPTIONS AND CONSTANTS:

- None

INPUTS:

- Ambient temperature and pressure: $T_a, P_a$
- Microturbine power output: $\dot{W}$
- Household power demand: $\dot{W}_h$

OUTPUTS:

- Secondary compressor discharge enthalpy and pressure: $h_{32}, P_{32}$
- Secondary compressor mass flow: $\dot{m}_{c2}$

DECISION CHART:

Figure 3-15: Secondary compressor decision chart.
THEORY:

When the accumulator requires charging, the secondary compressor draws power from the excess electrical power generated by the microturbine that is not consumed by household demand:

\[ \dot{W}_{c2} = \dot{W} - W_h \]  

(3-35)

For a given power input, volumetric flow was calculated using the digitized performance charts. This was translated into a mass flow using the following equation:

\[ \dot{m}_{c2} = \frac{P_a \dot{V}_{c2}}{RT_a} \]  

(3-36)

Isentropic efficiency is then calculated using curve fits from Figure 3-16.

Secondary compressor discharge temperature is then calculated using Equation (3-37). Nomenclature is given for Mode 2:

\[ T_{32} = T_{31} + \frac{T_{31}}{\eta_{c2}} \left( \frac{T_{32s}}{T_{31}} - 1 \right) \]  

(3-37)
3.3.4. Secondary expander

The IBC has the potential to operate with pressure ratios of 1 to 7, depending on the load demand of the household; higher electrical loads will require higher pressure ratios, while higher thermal loads will require higher mass flow rates. This range is significantly different from the pressure ratios of 3 to 3.76 experienced by the expander during microturbine operation. Hence a second expander with a design point tailored for typical mass flows and pressure ratios used in IBC operation is required to maximize efficiency. As station numbering is slightly different for Mode 1 and Mode 2, Mode 2 numbering will be used for this
ASSUMPTIONS AND CONSTANTS:

- $\eta_{e2} = 0.84$ at design for ISO standard atmospheric conditions
- Secondary expander discharge pressure is 2 percent above $P_a$
- No cooling flows

INPUTS:

- Ambient pressure: $P_a$
- Either household thermal ($\dot{Q}_h$) or electrical ($\dot{W}_h$) load
- Mode 1: accumulator discharge temperature: $T_{34}, (h_{34})$
  Mode 2: HEN discharge temperature: $T_{36}, (h_{36})$

OUTPUTS:

- Secondary expander discharge temperature: $T_{35}, (h_{35})$
- Secondary expander electrical and thermal outputs: $\dot{W}_{e2}, \dot{Q}_{e2}$
DECISION CHART:

Figure 3-17: Secondary expander decision chart.

THEORY:

For a given accumulator discharge temperature, the flow pressure into the secondary expander is throttled to adjust the mass flow according to Figure 3-19. This allows either electrical or thermal load following operation, depending on what is required. For operation in Mode 1, the secondary expander always follows household electrical demand. For Mode 2, the default mode is to follow household thermal demand. If the household electrical demand cannot be met while following the thermal demand, the secondary expander switches to an
electrical following mode to ensure all household loads are satisfied. Figure 3-18 graphically explains this process.

Once it has been decided which load is to be followed, a mass flow is guessed and a corresponding EPR and $\eta_{e2}$ is calculated using the secondary expander operating line map in Figure 3-19. Equations (3-38) and (3-39) are used to determine discharge temperature, then electrical and thermal outputs are determined using Equations (3-40) and (3-41) respectively:

$$\int_{T_{34}}^{T_{35}} \frac{C_p(T)}{T} dT - R \ln \left( \frac{P_{35}}{P_{34}} \right) = 0$$  \hspace{1cm} (3-38)
\[ T_{35} = T_{34} + T_{34} \eta_e \left( \frac{T_{35s}}{T_{34}} - 1 \right) \]  
\[ \dot{W}_{e2} = \dot{m}_{e2} (h_{34} - h_{35}) \]  
\[ \dot{Q}_{e2} = \dot{m}_{e2} (h_{35} - h_h) \]  

Figure 3-19: Off-design operating line for secondary expander.

3.3.5. Accumulator

The accumulator provides a method of storing energy when the microturbine is overproducing electrical load. It is charged with the secondary compressor and discharges to the secondary expander. The accumulator is well insulated, and is assumed to be installed inside the household.
ASSUMPTIONS AND CONSTANTS:

- Air in the accumulator is isothermal and isobaric
- A polytropic exponent of \( n = 1.2 \) was assumed for compression during charging and expansion during discharge (Appendix E explains the motivation behind selection of the polytropic exponent).
- Accumulator was assumed to be a horizontal cylinder with spherical end caps
- A free convection boundary condition is applied to the outer surface
- Accumulator internal surface temperature is equal to the bulk fluid temperature
- Fluid in the accumulator is quiescent
- Insulation thickness \( t = 0.1 \) m, insulation thermal conductivity \( k_{\text{ins}} = 0.038 \) W/mK, thermal resistance of the steel accumulator wall was treated as negligible
- Radiation heat transfer from the exterior surface of the accumulator is negligible
- Gravitational acceleration: 9.81 m/s\(^2\)

INPUTS:

- Household ambient enthalpy: \( h_h \)
- Discharging and charging mass flows: \( \dot{m}_{\text{out}} \), \( \dot{m}_{\text{in}} \)
• Charging enthalpy: $h_{in}$

OUTPUTS:

• Discharging enthalpy (accumulator bulk fluid enthalpy): $h_{out}$

• Heat loss: $\dot{Q}_\text{acc}$

• Accumulator pressure: $P_{acc}$

DECISION CHART:

Figure 3-20: Accumulator decision chart.

THEORY:

As the model was used in a time-based simulation, a set of equations had to be used that allowed variation in inlet mass flow and enthalpy while simultaneously calculating accumulator temperature and pressure. The 1st law of thermodynamics was applied to a control volume enclosing the accumulator where $e$ represents the specific energy of the system:

$$(Q + W + \sum mh)_{in} - (Q + W + \sum mh)_{out} = m_2 e_2 - m_1 e_1$$

(3-42)
The flow entering the accumulator is a moving fluid and does boundary work on the quiescent fluid in the accumulator. To account for this boundary work, specific energy of the fluid in the accumulator is measured using internal energy while specific energy of the incoming (or leaving) flow is measured using enthalpy. Heat addition or loss is present only in the form of heat transfer to ambient through the accumulator wall. Using these assumptions, a discrete form of Equation (3-42) can be written as:

$$\frac{\dot{m}_{\text{in}} h_{\text{in}} - \dot{m}_{\text{out}} h_{\text{out}} + m_1 u_1 - \dot{Q}_{\text{acc}}'}{m_1 + \dot{m}_{\text{in}} - \dot{m}_{\text{out}}} - u_1 = u_2 - u_1 = \frac{du}{dt} \quad (3-43)$$

With respect to Equation (3-43), subscripts 1 and 2 correspond to the accumulator state at the previous and current timestep respectively; this convention applies to all equations in this section. Pressure was modelled using a combination of differential forms of perfect gas law and the polytropic expansion relation:

$$\frac{dP_{\text{acc}}}{dt} = \frac{R}{V} \left( T_{\text{acc}} \frac{d m}{dt} + m_{\text{acc}} dT_{\text{acc}} \right) \quad (3-44)$$

$$\frac{dT_{\text{acc}}}{dt} = \frac{n - 1}{n} \frac{T_{\text{acc}}}{P_{\text{acc}}} dP_{\text{acc}} \quad (3-45)$$

Equations (3-44) and (3-45) are combined to form Equation (3-46):

$$\frac{dP_{\text{acc}}}{dt} = \frac{nRT_{\text{acc}}}{V} \quad (3-46)$$
An explicit discrete differential form is required to implement Equation (3-46) into a simulation marched in time:

\[
\frac{dP_{acc}}{dt} = (\dot{m}_{in} - \dot{m}_{out}) \left( \frac{nRT_1}{V} \right)
\]  
(3-47)

Finally heat loss (\(\dot{Q}_{acc}\)) must be estimated. Under a free convection assumption, the external convection coefficients must be estimated using empirical correlations. Equations (3-48) and (3-49) are averaged Nusselt number correlations for free convection around a horizontal cylinder [3.7] and a sphere [3.3] respectively:

\[
\overline{Nu_D} = \frac{1}{8} Ra_D^{1/3}
\]  
(3-48)

\[
\overline{Nu_D} = 2 + \frac{0.589 Ra_D^{1/4}}{\left(1 + \left[\frac{0.469}{Pr}\right]^{9/16}\right)^{3/9}}
\]  
(3-49)

Where the Rayleigh number is calculated as:

\[
Ra_D = \frac{g \beta (T_s - T_\infty) D^3}{\nu \alpha}
\]  
(3-50)

Equations (3-48) through (3-50) are then combined with Equation (3-51) to produce an estimate for the averaged convective heat transfer coefficient, one for the cylindrical surface and one for the spherical end caps.
\[
\bar{h} = \frac{Nu_p k}{D} 
\]  

(3-51)

Using the assumption that the heat transferred through the insulation via conduction is equal to the heat dissipated through free convection, Equation (3-52) is used to determine the external surface temperature of the accumulator where subscripts \(sp\) and \(cyl\) correspond to the spherical and cylindrical surfaces respectively:

\[
\frac{k_{ins}(T - T_s)(A_{sp} + A_{cyl})}{t} = \left[ (\bar{h}A)_{sp} + (\bar{h}A)_{cyl} \right] (T_s - T_\infty) 
\]  

(3-52)

\(\dot{Q}_{acc}'\) is then determined by back substituting \(T_s\) into Equation (3-52) and calculating the heat transfer through the accumulator wall or from the external surface of the accumulator via convection:

\[
\dot{Q}_{acc}' = \frac{k_{ins}(T - T_s)(A_{sp} + A_{cyl})}{t} = \left[ (\bar{h}A)_{sp} + (\bar{h}A)_{cyl} \right] (T_s - T_\infty) 
\]  

(3-53)

3.3.6. Individual generation system

Economic performance of the proposed system was compared against the performance of a natural gas furnace, vapour compression air conditioner, and purchasing grid power as is common in many North American and European households.
ASSUMPTIONS AND CONSTANTS:

- Natural gas furnace has a 1\textsuperscript{st} law efficiency of $\eta_f = 0.90$
- Air conditioner COP = 3 at $T_a = 27.8^\circ C$ and $P_a = 101.325 \text{ kPa}$
- Same energy rates used for trigeneration system were used for the individual generation system
- $LHV = 50 \text{ MJ/kg}$

INPUTS:

- Ambient temperature and pressure: $T_a$, $P_a$
- Household electrical and thermal loads: $\dot{W}_h$, $\dot{Q}_h$

OUTPUTS:

- $m_f|_f$
- $\dot{W}_{ac}$
THEORY:

Furnace performance was treated as invariant with changes to ambient temperature and pressure. Performance modelling was limited to calculation of furnace fuel consumption:

\[ \dot{m}_f \left|_f = \frac{\dot{Q}_h}{\eta_f LHV} \right. \]  \hspace{1cm} (3-54)

As the COP for most air conditioners is measured at an outside temperature of 27.8°C (82°F) as per Air-Conditioning and Refrigeration Institute (ARI) standard 210-240-2006 [3.1], the cooling load will be under-predicted at temperatures below 27.8°C, and over-predicted at temperatures above if COP is not allowed to vary with temperature. As a rule of thumb, for each degree the condensing
temperature is raised in a vapour compression cycle, the COP reduces by 2 to 4 percent (vice versa for each degree the condensing temperature is lowered) [3.2]. To mitigate the error introduced with a constant COP assumption at temperatures above the ARI nominal test conditions, a simple correction of 2.5 percent per degree Celsius [3.8] was applied to the design COP based on outside air temperature where the subscript nom indicates nominal ARI test conditions:

\[
COP = COP_{\text{nom}} \left[ 1 + 0.025(T_{\text{nom}} - T_a) \right]
\]  

(3-55)

Energy consumed by the air conditioner is then calculated using Equation (3-56):

\[
\dot{W}_{ac} = \frac{\dot{Q}_h}{COP}
\]

(3-56)

3.4. Description of simulation

The mathematical model of the system described in the previous section was incorporated into a SIMULINK™ simulation marched in time. This simulation provided control to the mathematical model to ensure a comfortable temperature was maintained throughout the simulated dwelling while remaining within operating envelopes of each system component, in addition to ensuring the household electrical demand was met.
3.4.1. Solver parameters

Household temperature profile was calculated using a bulk heat capacity calculated from Equation (3-57). The deviation of household temperature from the desired setpoint of 22°C (295 K) is determined using Equation (3-58).

Simulation control allowed household temperature to vary no more than ± 1.5°C from the nominal setpoint.

\[ C_h = \dot{m}_h C_{pa} \quad (3-57) \]

\[ \Delta T_h = \int \frac{\dot{Q}_{load} + \dot{Q} + \dot{Q}_{acc} + \dot{Q'}_{acc}}{C_h} \quad (3-58) \]

Several discretization schemes provided with SIMULINK™ were experimented with to arrive at a solver-independent solution, with the goal of optimizing solution accuracy and CPU time. With the exception of accumulator behaviour, trends in performance data were either linear or weakly non-linear in nature. As a result, higher order discretization schemes did not produce significantly different results from 1\(^{st}\) order schemes such as the explicit Euler method. As the control system was based on switches that turned on or shut off components abruptly, the simulation solver had to be able to deal with a high occurrence of discontinuities. The 1\(^{st}\) order Euler method using a fixed timestep was able to negotiate discontinuities without divergence.

It was desirable to choose as large a timestep as possible without significantly
affecting accuracy or inducing solver instability. A timestep of one second was chosen, as larger timesteps resulted in solution instability. This instability threshold can be attributed to the high rate of change in accumulator pressure during discharge as the IBC pressure ratio approaches atmospheric. At a lower pressure ratio, less specific work is produced by the expander hence a larger mass flow is required to satisfy a given electrical or thermal load. Accumulator pressure could drop below atmospheric between timesteps larger than one second, causing rapid solution divergence.

3.4.2. Demand scenarios

Controlling the system poses a significant programming challenge, as each component of the complex system must be monitored while ensuring ambient household temperature remains within a desired range. This is further complicated by a rapidly changing household electrical demand. With respect to the physical system, changing between modes requires redirection of flow through the heat exchanger network in addition to using different control logic; this could be accomplished with the use of solenoid actuated computer-controlled three way valves. As the control methodology is different from cooling to heating load production, they will be treated separately.
3.4.2.1. Cooling mode (Mode 2)

Controlling cooling operation is more difficult than controlling heating operation, as the system has greater difficulty cooling the household than heating it. This is primarily because the microturbine typically exhausts at roughly 800 to 900 K. This high-temperature exhaust provides a 550 to 650 K temperature difference compared to the household setpoint of 295 K. Conversely, the accumulator provides cooling exhaust at 200 to 294 K, which is only a 1 to 95 degree difference when compared to the setpoint temperature. As the control logic for the system can be confusing, perhaps the best way to illustrate the methodology is through an illustration. Figure 3-22 outlines the control logic used during a cooling mode of operation. The control can be broken into three main groups: 1) temperature recharge, 2) recharge, and 3) intermediate control.

1) Temperature recharge: This mode is engaged when the maximum setpoint temperature in the dwelling is reached. The system then engages the accumulator until the minimum setpoint temperature is reached. Drawing a parallel with common HVAC terminology, the temperature recharge mode is synonymous with a building cooling cycle.

2) Recharge: This mode is engaged when the accumulator minimum pressure has been reached. It overrides the temperature recharge mode, as if no accumulator pressure is left, the accumulator has no more cooling capacity left.
3) *Intermediate control:* This mode operates the microturbine or the accumulator (IBC) depending on the situation. The goal of this mode is to satisfy the electrical load, as the dwelling temperature is within the setpoint range during this mode and no recharge or temperature recharge cycle is engaged.
Figure 3-22: Process logic chart for cooling control
The red warning markers in Figure 3-22 are to indicate that under these control modes, there is the potential dwelling cooling demand can exceed system cooling power. If this occurs, dwelling temperature can rise above the maximum setpoint temperature. It is possible to size a system based upon such extreme operating conditions, however the efficiency throughout the remainder of the operation envelope would suffer from a severe system to dwelling mismatch. The key parameter in determining if the system will lag behind cooling demand is the ratio of accumulator recharge time to setpoint minimum to maximum time (SMMT). The SMMT is defined as the time it takes the dwelling to increase bulk air temperature from the minimum setpoint to the maximum setpoint via heat addition from the outside. Once the accumulator is fully discharged, it must be fully recharged before the next temperature recharge mode is engaged. If the accumulator is not fully recharged, a charging deficit is created that will continue to grow at each recharge phase until no cooling output is available. To prevent this, supplementary electrical power from the grid is fed to the secondary compressor to increase charging mass flow into the accumulator. The amount of additional electrical power required is such that accumulator recharge time is equal to the SMMT. By using such a ratio, the accumulator will not be charged before the maximum dwelling setpoint temperature is reached. This is desirable as the microturbine would have to run at off-design to satisfy household electrical demand if the accumulator was prematurely charged; gas turbines experience a
significant drop in thermal efficiency at part load, therefore part-load operation is avoided whenever possible. By using supplementary grid power, the system can be sized for an average cooling load rather than the maximum. If total energy islanding is required, household temperature will increase above the maximum setpoint limit during peak cooling load conditions as no supplementary electric power would be supplied to the secondary compressor.

3.4.2.2. Heating mode

Unlike the cooling mode of operation, there is no danger of household thermal demand exceeding system output while in a heating mode. There are however modes of operation that are extremely wasteful, and are highlighted in yellow in Figure 3-23. These modes are presented in one of two ways: the need off-design operation, or the need for heat bypass. Microturbine off-design operation is required when under a temperature recharge mode of operation and the accumulator is at maximum pressure. The heat load provided by the microturbine exhaust is still required to heat the dwelling, but the secondary compressor does not require any power as the accumulator is full. The microturbine therefore operates in an electrical load-following mode to ensure the power requirements of the dwelling are satisfied. Heat bypass is required when the inverse of the previous case is encountered. While under a recharge mode of operation, if the dwelling is at the maximum setpoint temperature, but the accumulator is not yet
at maximum pressure, heat must be dumped to the atmosphere; during the heat bypass mode, a fraction of the microturbine heat output is directed into the dwelling such that the dwelling temperature remains at the maximum setpoint temperature.
Figure 3-23: Flow chart for heating control logic
3.4.3. Load profiles

To perform a detailed economic evaluation of the proposed system, a full year of operation is simulated. To accomplish this, high-resolution load data was obtained using an open source program called ESP-r [3.4]. This was developed in part by the Energy Systems Research Unit at the University of Strathclyde in the UK. After decades of development, contributions from PhD theses, and several case studies, ESP-r has the ability to predict building thermal loads with a high degree of reliability. Factors such as solar gains, solar view factors, outside air infiltration, circulation, customizable duct and vent locations, lighting thermal gains, and occupant driven gains are incorporated into the model.

Figure 3-24: Geometry used in ESP-r to model thermal loads

Included in ESP-r is a basic CAD program that permits the user to build simple
geometry. This geometry is then used in modelling thermal loads. Figure 3-24 shows the geometry used in estimating annual household thermal loads for this study. The parameters chosen in ESP-r were designed to reflect construction practices common to single family detached dwellings constructed between the 1950s and 1980s:

- Occupied by a four-person family
- No basement, two story, 1500 ft$^2$
- Brick exterior walls with glass fibre insulation for a total RSI value of 2.19
- Ceiling of the secondary floor is insulated with an air gap for a total RSI value of 0.39
- Solar view factors typical of a suburban environment
- Double paned windows (2 x 3 ft.)
- Exterior surface of ground floor subjected to an averaged ground temperature profile for Winnipeg, Canada [3.10]
- Free air exchange between 1$^{st}$ and 2$^{nd}$ floor
- Outside air infiltration set at 1 air change per hour
- No internal walls
- Volume of air on each floor and attic varies in an isothermal manner
- Ambient temperature, wind, sunshine, and precipitation data for Winnipeg, Canada in 2001 were used
- Separate occupancy profiles used for weekdays and weekends
In addition, an occupancy profile was specified that included latent and sensible gains from body heat, appliances, showers/baths, and lighting. These profiles for weekdays and weekends can be found in Appendix B. Figure 3-25 is a sample of the output from the thermal simulation. While a full year was modelled in five minute increments, only data for January and July are presented to illustrate the magnitude of the largest heating and cooling loads required throughout the year.

The electrical profiles shown in Figure 3-25 were taken from a database maintained by the International Energy Agency called Annex 42 [3.5]. This program is a partnership between several governmental organizations and universities around the world. The electrical profiles used for the simulation represent the consumption of an average detached single family Canadian household, and was provided to Annex 42 by the Canadian Centre for Housing Technology based in Ottawa, Canada. The electrical profile includes consumption from air handling blowers used in furnace and air conditioning systems. Climatic data for Winnipeg, Canada was used for load simulation as this region experiences extreme cold and hot summers (-40°C to 40°C). This climate requires significant heating and cooling loads, making it ideal to test the performance of the trigeneration system under study.

In an effort to keep simulation development within a prescribed timeline, hot
water loads were not used in the simulation. As water can be heated with waste combustion exhaust, adding a hot water load will not incur any extra costs for the system under study. Conversely, providing a hot water load will increase costs for the independent generation system, making relative economic results from the simulation conservative.

Figure 3-25: Sample of loads estimated using ESP-r
Chapter 4
Simulation Results and Sensitivity Studies

4.1. Introduction

Developing the concept of hydraulic accumulation with an IFGT microturbine was an iterative process. The final system has evolved considerably from what was initially simulated. This section will describe the modifications made to the original system based on performance results.

4.1.1. Accumulator size

Since accumulator volume has no direct impact on turbomachinery or HEN sizing, it is easy to isolate the effect accumulator size variation has on system performance. The effect of volume variation was studied separately for Mode 1 and Mode 2, and are presented in descending order in Figure 4-1 through Figure 4-4. It was determined that the primary effect of accumulator volume variation is to increase or decrease cycling frequency; one cycle is defined as the period between microturbine shutdown to start-up.
Figure 4-1: Accumulator behaviour in Mode 1 for low load conditions. Accumulator volumes of 0.5, 1, and 2 m$^3$ are presented in descending order respectively.

Figure 4-2: Accumulator behaviour in Mode 1 for high-load conditions. Accumulator volumes of 0.5, 1, and 2 m$^3$ were used and are presented in descending order respectively.
As was expected, cycle frequency increased for high-load conditions for both configurations; however, under Mode 2 high-load conditions cycle frequency was significantly higher than for Mode 1 high-load. Figure 4-2 and Figure 4-4 (high-load) show a cycling frequency that would most likely be unachievable in practice for an accumulator volume of 0.5 m$^3$.

![Graph showing electrical and thermal load over time](image)

**Figure 4-3:** Accumulator behaviour in Mode 2 for low-load conditions. Accumulator volumes of 0.5, 1, and 2 m$^3$ were used and are presented in descending order respectively.

As the trigeneration system is controlled with components such as solenoid flow control valves, and intake and exhaust fans, rapidly cycling these components will lead to premature component failure and degradation of system performance due to more frequent transient operation. As transient responses were not
modelled (and the associated degradation to performance during start-up), there was no appreciable change to economic performance when accumulator size was varied.

Figure 4-4: Accumulator behaviour in Mode 2 for high-load conditions. Accumulator volumes of 0.5, 1, and 2 m³ were used and are presented in descending order respectively.

Selecting an appropriate tank size can based upon three considerations:

1) Minimum accumulator volume should be selected such that an actual system can operate at the maximum cycling frequency required throughout the year without abnormal degradation to system performance or component life. The maximum cycling frequency can be expected to
occur at peak thermal and electrical loads.

2) Larger accumulators will reduce the amount of transient operation, and by extension cycle frequency. This in turn will improve economic performance.

3) There is no recommended maximum accumulator size. Considerations to keep in mind when selecting an appropriate size are ease of installation and service, and cost.

4.1.2. HEN configuration

The Mode 1 schematic shown in Figure 3-2 was designed to utilize the highest system temperature as is practically possible to satisfy household heating loads. When a cooling load was required (Mode 2) high temperature expander exhaust was not required, expander exhaust was therefore dumped overboard. To improve the thermal efficiency of the HEN and microturbine system in Mode 2, different system configurations were designed for heating and cooling modes of operation,

Displayed in Figure 4-5 is electrical efficiency and SFC based upon electrical power output. Where Mode 1 lacks in electrical efficiency, it makes up for in production of thermal load. If the thermal load delivered to the household is taken into account in efficiency calculations, Mode 1 demonstrates a fairly flat total
efficiency of 93 to 95 percent from synchronous idle to full power.

![Graph showing thermal efficiency and SFC performance](image)

**Figure 4-5:** Comparison of thermal efficiency and SFC performance from full power to synchronous idle for HEN Mode 1 and Mode 2 configurations at standard ambient conditions of 101.325 kPa and 288K

When the microturbine is operating in heating mode, any losses due to turbomachinery isentropic efficiencies of less than unity are translated into increased flow temperature. This increased flow energy is not utilized if exhaust energy is vented to atmosphere. In the modelled system, any turbomachinery losses are recaptured when the exhaust is delivered to the household for space
heating purposes.

Mode 1 total efficiency losses can be attributed to pressure losses in the HEN and exhaust ducting, and due to mechanical, combustion, and electrical conversion efficiencies less than unity. This high overall efficiency is possible due to the implementation of the IFGT concept within the system, as the microturbine exhaust is free of combustion products and can be vented directly into the household. While operating in Mode 1, the microturbine and HEN are analogous to a high-efficiency natural gas furnace that produces electrical load as a by-product.

4.1.3. Microturbine size

The effect of varying the electrical output of the microturbine on economic performance and system response was investigated. To size the microturbine, compressor and expander maps were adjusted by varying corrected mass flows (compressor and expander) until the desired power output was achieved. Design and off-design PR and isentropic efficiency characteristics were left unchanged. It is acknowledged that this assumption will introduce some error in the smaller sizes, as isentropic efficiencies will degrade in smaller machines when compared to larger geometrically similar machines. It is believed that this error will not be significant enough to affect the conclusions drawn from the microturbine sizing
study. Three microturbine sizes were used for the sensitivity study: 5, 10, and 20 kWe. All component pressure temperature and power input and outputs were monitored to ensure the simulation was behaving as expected, however three key performance parameters were compared to determine the effect of microturbine size variation on system performance: fuel cost, accumulator behaviour, and household temperature. The latter two measures of performance were selected to give a measure of cycling frequency, and the corresponding effect on household temperature. While satisfying a heating load (as in Mode 1), microturbine size had a negligible effect on cost. This may seem counterintuitive given the fact that for the same accumulator pressure, larger microturbine sizes demonstrated higher accumulator temperatures as seen in Figure 4-6.

Higher accumulator temperatures translate to less fuel required to bring accumulator discharge flow up to temperature through the HEN, and therefore reduces SFC during IBC operation. The higher accumulator temperature should therefore translate to a reduction in fuel costs. A more in-depth look into how the system charges the accumulator is required to explain this phenomenon. Household electrical load varies between zero and about 6 kWe, which means with the exception of the 5 kWe engine, the microturbine is always overproducing electrical load at full load. Excess load is fed to the secondary compressor, which then charges the accumulator. The secondary compressor was sized to ensure
maximum isentropic efficiency was achieved for average levels of microturbine overproduction (secondary compressor input power) based on a 10 kWe engine, shown in Figure E-11.

Figure 4-6: Effect of microturbine size on system behaviour. Operating costs, accumulator temperature, and pressure compared for three different microturbine sizes while satisfying a heating load (Mode 1).

The 20 kWe engine supplies more input power to the secondary compressor than the 10 kWe engine, and is therefore not matched for maximum isentropic efficiency. The secondary compressor sends flow to the accumulator at a higher
temperature with larger engines due to the lower efficiencies demonstrated at higher secondary compressor mass flows.

Figure 4-7: Household temperature response for three different microturbine sizes while satisfying a heating load (Mode 1).

A higher specific work is required by the secondary compressor as well, which negates the benefit of a lower HEN SFC for the 20 kWe engine. This validates the claim made in the previous Section (4.1.1), that any losses due to turbomachinery isentropic efficiencies of less than unity are recuperated later either via reduced HEN SFC or an increase in thermal load provided to the
Microturbine size had very little impact on system performance while operating with Mode 2; Figure 4-8 and Figure 4-9 show negligible impact on system behaviour and household temperature response. Operating cost was not influenced by microturbine size either. All three microturbine sizes could not produce sufficient excess power to supply the secondary compressor to meet household cooling demands during peak periods (greater than 2 kWt). This meant that during peak periods supplementary grid power was purchased to
increase secondary compressor mass flow; hence the accumulator was charged at the same rate despite engine size during peak cooling periods. This translates to similar accumulator temperature and pressure behaviour for all three engine sizes as shown in Figure 4-8.

Figure 4-9: Household temperature response for three different microturbine sizes while satisfying a cooling load (Mode 2).

Based upon this study, the only consideration required when choosing a microturbine size is to ensure the engine can satisfy peak electrical loads while
providing a power input to the secondary compressor. This will ensure total energy islanding can be attained for Mode 1, and for Mode 2 (if a higher household setpoint temperature is acceptable during peak summer temperatures). The 10 kWe engine is therefore recommended, as the 5 kWe engine cannot satisfy peak electrical loads, and no benefit is realized from choosing the more expensive 20 kWe microturbine.

4.1.4. Microturbine bleed

In an effort to reduce system complexity and cost, initial design called for the accumulator to be charged with microturbine compressor bleed flow instead of a secondary compressor, as shown in Figure 3-1. The microturbine compressor was run at design conditions with output power controlled by throttling compressor discharge bleed flow. This allowed the microturbine to operate in an electric load following manner, while simultaneously charging the accumulator and satisfying a heating load. While satisfying a heating load, fuel costs for the system using compressor bleed flow to charge the accumulator were slightly higher than if a secondary compressor was used, as shown in Figure 4-10. The difference in cost is due to the fact that the time to increase household setpoint temperature from minimum to maximum limits was sometimes less than the time required to charge an empty accumulator. To prevent household overheating, expander exhaust was discharged to atmosphere while waiting for the
accumulator to charge, reducing the overall efficiency of the system. This has been observed to occur during low thermal high electrical load conditions; a high electric load will reduce bleed flow into the accumulator, as the microturbine must pass more mass flow through the expander to satisfy the higher electrical demand; this translates into a longer accumulator charging period. If the thermal demand is low, expander exhaust will have to be dumped overboard due to the longer charging period if bleed flow is used to charge the accumulator.

Figure 4-10: Fuel costs for Mode 1 (heating load), comparison is made between microturbine operation with compressor bleed versus using a secondary compressor. Natural gas is set at 6.2 CAD/GJ.
Cost data for the cooling mode is not displayed as microturbine bleed flow was not able to satisfy household cooling requirements as shown in Figure 4-11; using bleed flow limits maximum cooling capacity to less than about 0.75 kWt for a 10 kWe engine. The trigeneration system can satisfy a cooling load as long as the accumulator charging flow is equal to the discharge flow. When the system cannot recharge the accumulator as fast as it is emptied, the household setpoint temperature exceeds the maximum setpoint limit, as is the case in Figure 4-11.

Figure 4-11: Household setpoint deviation using microturbine bleed flow to charge the accumulator while satisfying a cooling load. Red dotted lines indicate household minimum and maximum setpoint temperatures (22 ± 1.5°C)
The microturbine compressor size is based upon a specified engine design point and has to be matched with the expander. As a result, the only way to increase microturbine maximum compressor bleed flow without changing turbomachinery isentropic efficiencies or pressure ratios is to increase the size of the engine. It is possible that a sufficiently large engine could provide the cooling load required, however it would be severely oversized for heating load production. Figure 4-12 illustrates the benefit realized by the addition of a secondary compressor. The secondary compressor does not have to be matched with another component, nor does it have to operate at a continuous speed.

![Graph](image)

Figure 4-12: Variation in accumulator charging flows with household electrical load for various ambient temperatures. Data for microturbine bleed mass flow is for a 10 kWe engine.

The secondary compressor used in the simulation also demonstrates significantly
higher isentropic efficiencies (up to 0.92) when compared to the microturbine compressor (0.75 at design). When in a constant pressure mode of operation, this higher efficiency translates to higher mass flows for the same input power. The secondary compressor also has the benefit of being able to accept grid power if necessary to boost mass flow. This ensures no accumulator flow deficit exists, thereby maintaining household temperature within setpoint limits.

A typical operating line for a gas turbine in constant speed mode of operation is almost vertical on a graph of corrected compressor mass flow versus CPR; hence compressor mass flow is virtually invariant from full power to synchronous idle. If bleed flow is to be boosted without using a separate compressor or resizing the microturbine, the engine must deviate from constant speed operation. During peak loads compressor mass flow, and by extension bleed flow, could be boosted by supplying grid power to the high-speed generator; at the same time household electrical demand could be supplied by grid power as well. Supplying grid power to the high-speed generator would increase shaft power to the compressor and increase CPR; this in turn would permit a larger maximum bleed flow. This concept was not modelled or simulated, and remains a topic of further investigation. It is always desirable to reduce system complexity and maintenance costs; any concept that involves elimination of the secondary compressor is worth pursuing.
4.1.5. #4 Heat exchanger

Heat pumps and geothermal systems have benefited from the pseudo-infinite heat capacity deep in-ground installations offer for many years. A study was conducted to evaluate the effect a deep in-ground heat exchanger would have on the economic performance of the system under study. Labelled as '#4 Hx' in Figure 3-2 and Figure 3-3, this heat exchanger is buried in-ground such that the surrounding mass remains a constant 8°C year round (see Section 3.1). The #4 Hx was used in a different manner for Mode 1 and 2:

Mode 1: Secondary compressor inlet flow is pre-heated by drawing inlet flow through #4 Hx

Mode 2: Secondary compressor discharge flow is cooled through #4 Hx before entering the accumulator.

As shown in Figure 4-13, #4 Hx provides a significant benefit for operation in Mode 2. Without #4 Hx, the accumulator temperature demonstrates stagnation temperatures of up to 450 K, as secondary compressor discharge is not allowed to cool (not shown in Figure 4-13). It is possible that even after expansion through the IBC, exhaust flow temperature is above ambient household temperature. When this happens no cooling load can be provided by the system and household temperature increases above setpoint limits. Not only does #4 Hx provide a substantial economic benefit, it is required to satisfy the mission of the
trigeneration system while operating in Mode 2.

![Graph: Cost (CAD) vs Time (days) for Cooling and Heating Modes]

Figure 4-13: Fuel and purchased grid power costs for trigeneration operation with and without #4 Hx in Mode 1 and Mode 2 modes of operation.

This economic benefit is not extended to operation in Mode 1, as there is negligible improvement in economic performance. It is believed that the benefit of an elevated accumulator temperature is offset by the reduced mass flow through the secondary compressor associated with less dense inlet flow. Since the system is designed to charge the accumulator until a maximum pressure has
been reached, any reduction in mass flow into the accumulator during charging will increase the time required until fully charged. This translates into longer microturbine run times and increased fuel consumption. Of course this increase in microturbine fuel consumption is offset by a decrease in HEN fuel consumption due to higher accumulator temperature; the results shown in Figure 4-13 indicate that this offset is equal in magnitude. To reduce unnecessary wear and tear on the #4 Hx, it is therefore recommended that the #4 Hx be used for Mode 2 only.

4.1.6. IBC flow treatment

To extract more specific work from the IBC expander, the effect of increasing expander inlet temperature (EIT) was investigated. Two cases were studied: the first case did not cycle accumulator discharge flow through the HEN. As accumulator discharge flow is typically anywhere from 300 to 400 K, secondary expander discharge flow temperature was too low to provide a useful thermal load. The second case increased accumulator discharge temperature by cycling through the HEN before entering the secondary expander. The HEN was fired at a constant maximum combustion temperature (T23) of 1200 K for all accumulator discharge pressures and flow rates. Despite consuming fuel during IBC operation, cycling accumulator discharge flow through the HEN reduced overall fuel consumption as shown in Figure 4-14. While the cost savings may seem marginal, note that the data in Figure 4-14 spans only a week. Fuel savings over
a three to four month winter season with high thermal load are quite substantial. Another benefit of increasing IBC cycle temperature is that HEN thermal cycling is reduced. Wear and tear placed upon heat exchanging equipment within the HEN by repeatedly heating up and cooling off is dramatically reduced, as the HEN is not allowed to cool off when operating in Mode 1.

![Graphs showing thermal and electrical load](image)

Figure 4-14: Trigeneration system economic performance with and without increasing EIT. Maximum HEN combustion temperature of $T_{23} = 1200$ K was kept constant throughout IBC operating envelope.

By continuously keeping the HEN at an elevated temperature, error introduced by
not modelling transient heat exchanger behaviour is reduced. Maximum heat exchanger effectiveness is achieved only when energy accumulation within the components of the HEN goes to zero. If accumulator discharge is not cycled through the HEN, it will cool down. When the microturbine is started up again, there will be a brief period where the HEN is not operating at design effectiveness while internal components absorb energy from the two flows passing through. It is recommended that accumulator discharge flow be cycled through the HEN (which is to be fired at the highest possible temperature) in Mode 1, before discharge to the secondary expander. Accumulator discharge should be vented directly through the secondary expander in Mode 2.

4.1.7. Secondary expander

The microturbine expander must be matched with the compressor in such a manner as to produce a desired power output at design. These restrictions dictate the expander characteristic as seen in Figure 3-14. As a rule of thumb, the compressor consumes roughly two units for every one unit of shaft output in a traditional Brayton cycle [4.1]. Hence the expander characteristic is not always ideal for IBC operation given that the compressor is not consuming two out of every three units produced by the expander. It has already been determined that increasing accumulator discharge flow temperature improves economic performance (see Section 4.1.6), however this poses a challenge for maintaining
If accumulator discharge was passed through the HEN while adding sufficient fuel to bring the HEN combustion side temperature to its maximum, the thermal output from the microturbine expander had the potential to exceed the household heating load. For the household temperature to remain within setpoint limits, the thermal load delivered to the household during IBC operation has to be less than the household thermal load. This controlled household cool down allows microturbine exhaust to be used for heating purposes when recharging the accumulator.

![Figure 4-15: Ratio of electrical to thermal output of the IBC expander at maximum HEN firing temperature \( T_{23} = 1200 \text{ K} \) (EIT = 1163 K).]
If the household temperature is too high when the microturbine engages an accumulator recharge cycle, exhaust will have to be dumped overboard to prevent household overtemp. At the same time to minimize fuel costs, IBC maximum cycle temperature \( (T_{23}) \) must be kept as high as possible. Figure 4-15 shows the relationship between thermal and electrical output of the IBC using the microturbine expander, and a separate re-sized secondary expander. The secondary expander used is geometrically similar to the microturbine expander with a scaling factor applied such that the corrected mass flow is 1/6th of the microturbine expander. Household heating loads during severe winter months typically vary between 8 and 15 kWt. Figure 4-15 shows secondary expander thermal output is almost always below this demand, yet is sufficiently sized to provide for peak household electrical demand of about 7 kWe. Using the re-sized secondary expander allows the HEN to be fired at maximum temperature for improved economic performance while not exceeding household thermal demand.

### 4.2. Final results

Based upon the results from the studies described in Section 4.1, a final configuration was selected for maximum economic performance. See Figures Figure 3-2 and Figure 3-3 for schematics of the final configurations for Mode 1 and Mode 2. Key design points are summarized as follows:
- Accumulator size was set at 2 m$^3$. The dimensions of such an accumulator (1.37 x 1.37 m) should not pose significant practical problems for installation in new and old construction alike. Larger sizes are preferred if cost permits.
- The HEN operates in heating and cooling modes (Mode 1 and Mode 2).
- Microturbine design point electrical output at ambient conditions of 101.325 kPa and 288 K is 10 kWe.
- Secondary compressor discharge is cycled through #4 Hx in Mode 2. #4 Hx is not used in Mode 1.
- IBC flow is cycled through a secondary expander which has a design corrected mass flow that is $1/6^{th}$ of the microturbine expander.
- IBC flow is cycled through the HEN that is fired at maximum temperature when a heating load is required.

Figure 4-16 is a comparison of yearly energy consumption for the final trigeneration system configuration and the independent generation system. A severe penalty is paid by the system during summer operation, as natural gas consumption reduces only slightly while consuming electricity at the same time. Figure 4-17 breaks down economic performance by month, better illustrating the relative performance of the two systems throughout the year. Supplemental electrical power is required for the trigeneration system during periods of high cooling load demand, accounting for half of yearly independent generation
consumption; hence the high monthly operating cost for the trigeneration system during summer months, shown in Figure 4-17. These results show that system performance during heating load production is potentially superior to independent generation (depending on market energy prices). There is much room for improvement during cooling load production, further study is currently being conducted to improve economic performance. Eliminating supplemental electrical power consumption is one means of doing so.

Figure 4-16: Yearly consumption of electricity and natural gas for the trigeneration and independent generation systems.
Figure 4-17: Monthly operating cost comparison between the trigeneration and independent generation systems.

Total elimination of supplemental electrical power not only brings an economic benefit, but energy islanding could be achieved for the full year. The solution lies in increasing the specific cooling output (defined as kW of energy input per kW of cooling produced). This can be accomplished in a number of ways, however it is believed that increasing the isentropic efficiency of the secondary compressor and expander would have the most impact. The primary source of thermal inefficiency within the trigeneration system during cooling load production is the heat lost through the #4 Hx. At design, the secondary compressor has a peak isentropic efficiency of 0.92 for a volume flow rate of 0.039 to 0.043 m$^3$/s. During
peak cooling load production, the volume flow rate increases to as much as 0.110 m^3/s with a corresponding isentropic efficiency as low as 0.64; the secondary compressor is clearly optimized for lower flow rates. During heating load production, a low isentropic efficiency is not a penalty to economic performance as the additional heat added to the compressed air is recovered later as a heat load. Low isentropic efficiencies are a penalty during cooling load production, as any excess heat added to secondary compressor flow is removed through the #4 Hx. If a compressor is optimized for operation close to its maximum flow rate, it is believed that specific cooling output would increase. A similar argument is made for the secondary expander. With a higher isentropic efficiency, expander discharge temperatures will be lower. The secondary expander typically operates at pressure ratios between 1.05 and 2.5 with a corresponding variation in isentropic efficiency of about 0.76 to 0.83 (see Figure 3-19). Modern aerodynamic design has allowed radial turbines to achieve isentropic efficiencies in excess of 0.92 [4.7]; hence there is much room for improvement in the current design.

Electrical efficiency is not a concern when satisfying a heat load, as a reduction in electrical output translates to a proportional increase in heat load output. Electrical efficiency is a concern when satisfying a cooling load, as any reduction in electrical output due to a decrease in electrical efficiency mean less power is
provided to the secondary compressor; hence the accumulator takes longer to charge. While the HEN is effective in extracting energy from microturbine expander exhaust, combustion flow from the HEN is still discharged at about 510 K and microturbine exhaust is discharged at about 350 K in Mode 2. Future iterations of the simulation will use these flows to provide a hot water load without an increase in fuel consumption. As the independent generation system would require additional fuel or electricity to satisfy a hot water load, the difference between the economic performance of the trigeneration and independent systems would decrease.

In an effort to ensure results were not unrealistically optimistic, microturbine parameters such as PR, maximum cycle temperature, and component isentropic efficiencies were selected to be conservative. An upper limit for microturbine compressor and expander efficiencies of 0.85 and 0.90 respectively could be used, however the economic performance was not investigated. Perhaps the largest potential gain to system electrical efficiency can be achieved by uprating the HEN.
Table 4-1: Effect of increasing maximum \#2 Hx temperature (T_{23}) on microturbine electrical efficiency in Mode 2. Values are for ambient conditions of 288 K 101.325 kPa.

<table>
<thead>
<tr>
<th>Max HEN Temp (K)</th>
<th>Electrical Efficiency</th>
</tr>
</thead>
<tbody>
<tr>
<td>1200</td>
<td>30.6</td>
</tr>
<tr>
<td>1300</td>
<td>34.3</td>
</tr>
<tr>
<td>1400</td>
<td>35.7</td>
</tr>
<tr>
<td>1500</td>
<td>37.4</td>
</tr>
</tbody>
</table>

A conservative value for maximum HEN temperature was selected (T_{23} = 1200 K), to ensure a reasonable service life for Hx \#2. Use of high temperature materials and special design would permit an increase to the maximum cycle temperature. Table 4-1 shows the efficiencies possible with a temperature uprate. Note that these results were obtained without modifying compressor or turbine characteristics. For temperatures other than the design maximum temperature of 1200K, the compressor and expander selected for this study will be operating in off-design at 100 percent power with an associated penalty on isentropic efficiency. The values in Table 4-1 are therefore lower than what would be achieved with turbomachinery that has been sized specifically for the new maximum temperature.

4.2.1. Market variation study

Using 2007 market energy prices for Winnipeg, Canada, household thermal loads were estimated. Results from Figure 4-16 were used to arrive at a yearly economic performance comparison between the modelled and independent generation systems shown in Figure 4-18. Two key conclusions can be made
based upon Figure 4-18: 1) The trigeneration system is superior to individual generation while producing a heat load. 2) The independent generation is superior while producing a cooling load. With electricity charged at 5.7 CAD/MWh and natural gas at 8.2 CAD/GJ, the independent generation system was 48 percent less expensive to run for one year when compared to the trigeneration system. The effect of market price variation on economic performance was investigate. Figure 4-19 is a plot of projected natural gas and electrical prices for Winnipeg, Canada (the same city used to predict thermal loads in ESP-r). The projections in Figure 4-19 are averages of the results from four independent studies commissioned by Natural Resources Canada [4.6].

![Figure 4-18: Yearly cost comparison between the trigeneration and independent generation systems using 2007 market data from Figure 4-19.](image-url)
Figure 4-19: Historical and projected household natural gas and electricity prices. [4.1]

Table 4-2: Projected economic performance of the trigeneration and independent generation systems. Market prices are based on projections from Figure 4-19.

<table>
<thead>
<tr>
<th>Year</th>
<th>CAD/GJ</th>
<th>CAD/MWh</th>
<th>NG cost</th>
<th>Elec. cost</th>
<th>Total cost</th>
<th>NG cost</th>
<th>Elec. cost</th>
<th>Total cost</th>
<th>% less</th>
</tr>
</thead>
<tbody>
<tr>
<td>2007</td>
<td>8.2</td>
<td>5.7428</td>
<td>2805</td>
<td>277</td>
<td>3082</td>
<td>1096</td>
<td>521</td>
<td>1618</td>
<td>48</td>
</tr>
<tr>
<td>2011</td>
<td>7</td>
<td>6.2244</td>
<td>2394</td>
<td>300</td>
<td>2695</td>
<td>936</td>
<td>565</td>
<td>1501</td>
<td>44</td>
</tr>
<tr>
<td>2015</td>
<td>7.4</td>
<td>6.7060</td>
<td>2531</td>
<td>324</td>
<td>2855</td>
<td>989</td>
<td>609</td>
<td>1598</td>
<td>44</td>
</tr>
<tr>
<td>2019</td>
<td>8.5</td>
<td>7.1876</td>
<td>2908</td>
<td>347</td>
<td>3254</td>
<td>1136</td>
<td>653</td>
<td>1789</td>
<td>45</td>
</tr>
</tbody>
</table>

Economic performance was then evaluated based upon projected market data. Unfortunately, projected economic performance does not change appreciably as
shown in Table 4-2. To favourably change economic performance for the trigeneration system based on market price alone, natural gas prices must fall while electricity prices remain constant or increase. This has not been the trend in Canadian markets, and is not expected to change in the future [4.1].

Energy prices from international markets that have regions of similar climate to Winnipeg, Canada were compared in Table 4-3 to see if a different energy market has an impact on economic performance. All regions studied still predicted the independent generation system would outperform the trigeneration system economically, however there was some degree of variation. Western European countries and the United States demonstrated similar results showing the economic performance of independent generation is about 35 to 47 percent better than the trigeneration system; similar to the results obtained for Winnipeg, Canada.

It is particularly interesting to note the difference in economic performance between the western world and the former Soviet Union. Russia’s Gazprom is the primary supplier of natural gas to Europe, and has flooded the Russian market with cheap natural gas. The dramatically lower natural gas prices in Russia create a favourable economic climate for the trigeneration system. In addition, peak cooling loads are less for the more populated regions of Russia, as summer temperatures are lower than the Canadian prairies. Due to a pre-World War two
electricity-generating infrastructure, reluctant international, and heavy public utility regulation, Russia is facing a shortage in capacity.

Table 4-3: Yearly economic performance of the trigeneration and independent generation systems for international markets. Market prices are for 2006 [4.5][4.6][4.3][4.2].

<table>
<thead>
<tr>
<th>Country</th>
<th>Market Prices</th>
<th>Trigeneration</th>
<th>Independent Generation</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>CAD/GJ</td>
<td>CAD/MWh</td>
<td>Cost</td>
</tr>
<tr>
<td>US</td>
<td>13.02</td>
<td>10.4</td>
<td>4956</td>
</tr>
<tr>
<td>Finland</td>
<td>8.42</td>
<td>12.8</td>
<td>3498</td>
</tr>
<tr>
<td>Switzerland</td>
<td>18.3</td>
<td>13.3</td>
<td>6902</td>
</tr>
<tr>
<td>Czech Rep.</td>
<td>12.99</td>
<td>12.2</td>
<td>5032</td>
</tr>
<tr>
<td>Romania*</td>
<td>4.3</td>
<td>11.6</td>
<td>2031</td>
</tr>
<tr>
<td>Russia*</td>
<td>0.54</td>
<td>4.92</td>
<td>422</td>
</tr>
</tbody>
</table>

* market prices are for 2004, 2006 prices were unavailable

In an effort to fund modernization, Russia's electrical tariffs have already jumped 15 percent in 2007, with another 10 percent increase planned next year [4.3]. This dramatic increase in electricity rates is not expected to affect natural gas prices, which are expected to increase at the nominal rate of inflation. This trend will serve to make the trigeneration system more attractive from the standpoint of the consumer and investors. International investment firms or companies interested in capitalizing on the lack of capacity in Russia's electricity grid would be much more interested in selling stand alone units to consumers, rather than invest in large infrastructure and then have to deal with tariff regulation.
4.3. Validation

Modules contained within the in-house model and simulation were externally verified to provide a measure of confidence in conclusions made. A description of the methodology used, and results from the validation studies performed can be found in Appendix E.
Chapter 5
Component Selection and Conceptual Design

5.1. Introduction
Simulating and modelling physical systems gives valuable information about
system behaviour, economic performance, and parameter sensitivity without the
need of costly prototyping processes. A simulation may produce favourable
results that lead to promising conclusions, but practical considerations prevent
prototyping. The conclusions drawn in Chapter 4 are invalid if the modelled
system has significant practical challenges. These challenges can present
themselves in high component purchase costs, high design costs for specialized
equipment, and unfavourable market conditions to name a few. The following
chapter will investigate if any such challenges are foreseen for the trigeneration
system, and suggest solutions.

5.2. Microturbine
One of the strengths of the trigeneration system under study is the fact that the
majority of the components used employ proven industry tested technologies; the
microturbine is a good example of such a component. While there are several
companies that produce commercial microturbine packages, none produce an
engine with an output of less than 30 kW. The mathematical model assumes a microturbine output at design of 10 kWe, which does not exist as an off-the-shelf purchase. While there are other microturbines available for purchase than those listed in Table 5-1, the units listed therein span the full range of microturbine power sizes offered.

Despite the lack of microturbine packages in the required size, small-scale compressor and expander technology is widely available in a different form. Turbochargers have been used for decades to increase specific power output from spark and compression ignition engines. Turbochargers do not produce a useful work output, as all work generated by the turbine goes into compressing engine inlet air, however radial turbomachinery and housings could be adapted to

<table>
<thead>
<tr>
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<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Electrical efficient (%)</td>
<td>26</td>
<td>28</td>
<td>32 (Target)</td>
<td>26</td>
<td>18</td>
<td>35 (Target)</td>
<td>28</td>
</tr>
<tr>
<td>Output power (kWe)</td>
<td>30</td>
<td>60</td>
<td>250</td>
<td>50</td>
<td>295</td>
<td>175</td>
<td>80</td>
</tr>
<tr>
<td>Mass flow rate (kg/s)</td>
<td>0.31</td>
<td>0.49</td>
<td>1.84</td>
<td>0.48</td>
<td>2.0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Pressure ratio</td>
<td>6.1</td>
<td>3.5</td>
<td>6.7</td>
<td>6.7</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Axial speed (rpm)</td>
<td>96,000</td>
<td>96,000</td>
<td>45,000</td>
<td>80,000</td>
<td>49,000/35,000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>TIT (°C)</td>
<td>840</td>
<td>927</td>
<td>940</td>
<td>940</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Exhaust temp. (°C)</td>
<td>275</td>
<td>370</td>
<td>271</td>
<td>580</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Exhaust pressure (kW)</td>
<td>85</td>
<td>150</td>
<td>161 (Hot water)</td>
<td>1074 (Steam)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NOx (ppmv)</td>
<td>&lt;9 (15%O₂)</td>
<td>&lt;9 (15%O₂)</td>
<td>&lt;9 (15%O₂)</td>
<td>&lt;15 (16%O₂)</td>
<td>&lt;19 (16%O₂)</td>
<td>≤10 (15%O₂)</td>
<td>≤25 (15%O₂)</td>
</tr>
<tr>
<td>Fuel</td>
<td>Natural gas</td>
<td>Natural gas</td>
<td>Natural gas</td>
<td>Town gas 13A, LPG, Kerosene</td>
<td>Town gas 13A</td>
<td>Natural gas</td>
<td>Natural gas, LPG, Propane, Butane</td>
</tr>
<tr>
<td>Maintenance interval (h)</td>
<td>8,000</td>
<td>12,000</td>
<td>12,000</td>
<td>11,000</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Life time (h)</td>
<td>48,000</td>
<td>48,000</td>
<td>45,000</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Sound level (Package)</td>
<td>65 dBA @ 10 m</td>
<td>72 dBA @ 10 m</td>
<td>72 dBA @ 1 m</td>
<td>70 dBA @ 1 m</td>
<td>70dBA @ 1 m</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Unit cost ($/kW)</td>
<td>≤$500/kW (Target)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 5-1: Summary of specifications for commercially available microturbines [5.18]
function as a microturbine. The Garrett GT22 series turbocharger, with a compressor input power of 15 to 25 kW offers a good basis from which to build a suitable microturbine, see Appendix C for component maps for the GT22 series turbocharger.

As seen in Figure 5-1, the trigeneration system requires a special microturbine powertrain design that incorporates clutches to allow each component to operate independently of another. The modular construction of this drive train makes for easy fabrication and modification of an existing microturbine design, without significant alterations to the microturbine casing or exhaust manifold.

5.3. Heat exchangers

5.3.1. High-temperature heat exchanger (#2 Hx)
The fired heat exchanger (#2 Hx) is similar in appearance to a common household natural gas furnace, however the operating pressure and temperature is significantly higher. This requires alternate materials and design to ensure an adequate service life is achieved. As the exchanger will be subject to a high rate of thermal cycling, reducing cracking and fatigue due to thermal expansion is of paramount importance in a successful design. Exchanger designs using plates and thin metal membranes such as plate fin, plate, and spiral constructions would most likely not be able to withstand burner operating temperatures (1200K) without some degree of warp and/or cracking. Ceramic heat exchangers show signs they may be able to be adapted for use in a fired exchanger with high thermal cycles. Exchangers fabricated from SiC exhibit very low thermal expansion coefficients, have good strength at elevated temperatures and have very low heat capacities [1.44]. SiC would be ideally suited for systems that are frequently cycled due to the very high thermal conduction coefficient (which exceeds copper and almost doubles aluminium). This would allow the exchanger to be brought up to temperature rapidly. Although ceramic heat exchangers have been in use for some time, their application to compact heat exchangers is still in the experimental phase. As they are unproven in both performance and cost, ceramic heat exchangers will not be considered for use in the fired heat exchanger module for this study. Directly fired heat exchangers are typically built to order, hence the few companies that do make them do not have a standard
product line from which to choose. Fired exchangers are typically seen in the oil and gas or mining industries as process re-heaters to keep process fluids up to temperature. Such an application generally requires a very large unit, an example is shown in Figure 5-2, making the unit required for this study a special order. As design and procurement of the fired exchanger is outside the scope of this thesis, companies were not pursued to obtain quotes.

Figure 5-2: Directly fired heat exchanger fabricated by Selas Fluid for the oil and gas industry [5.9]

5.3.2. Low-temperature heat exchangers (#1 and #3 Hxs)

Unlike exchanger #2, the two non-fired exchangers used in the system (#1 and #3) can be purchased off-the-shelf due to lower operating temperatures, and due
to the fact that they operate with a common gas-to-gas exchange process. Table 5-2 lists the operating temperatures of the heat exchangers in the HEN; Figure 3-2 and Figure 3-3 show the locations of the heat exchangers within the modelled system. Evaluation and selection of heat exchanger construction was subject to the following design constraints for exchangers #1 and #3:

- Must be able to withstand sustained maximum operating temperatures as listed in Table 5-2.
- Must demonstrate a service life of 10 to 15 years of normal operation.
- Must be resistant to degradation due to high thermal cycling during operation.
- Must demonstrate an effectiveness of 85 percent or higher, 90 percent is preferred.
- Unit cost must be realistic for purchase by a household consumer.

This evaluation process identified the following heat exchanger classifications as potential candidates for use as non-fired exchangers in the subject system: brazed plate, shell and tube, plate fin, and regenerators.

**Table 5-2: Heat exchanger operating temperatures for an OAT of 288 K**

<table>
<thead>
<tr>
<th></th>
<th>Hx #1</th>
<th></th>
<th>Hx #2</th>
<th></th>
<th>Hx #3</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>In</td>
<td>Out</td>
<td>In</td>
<td>Out</td>
<td>In</td>
<td>Out</td>
</tr>
<tr>
<td>Air Side (K)</td>
<td>452</td>
<td>830</td>
<td>830</td>
<td>1164</td>
<td>513</td>
<td>839</td>
</tr>
<tr>
<td>Comb. Side (K)</td>
<td>868</td>
<td>513</td>
<td>1200</td>
<td>868</td>
<td>897</td>
<td>491</td>
</tr>
</tbody>
</table>
5.3.2.1. Brazed plate heat exchanger

The brazed plate heat exchanger (BPHE) typically uses a series of corrugated plates stacked together to deliver compact and effective heat transfer. Unlike a gasketed plate heat exchanger, these plates are brazed together in a vacuum furnace. This permits higher temperature operation due to the presence of high temperature nickel alloy braze in lieu of elastomer gaskets. As one fluid passes through every other gap provided by adjacent plates, large amounts of heat transfer surface are provided in a small package, shown in Figure 5-3.

Figure 5-3: Illustration of alternating fluid pattern for a three fluid BPHE [5.25]
BPHEs offer very high heat transfer performance due to low velocities and high turbulence induced by rapidly changing flow directions; high turbulence also contributes to reducing fouling, effectively increasing service life [5.22]. When combined with a large heat transfer surface area, plate exchangers can achieve fluid exit temperature differentials of 0.5 to 1 K [5.13]. Due to the simple modular construction of the BPHE, capital costs are very low compared to equivalent shell and tube exchangers. Although brazing plates together raises the allowable operating temperature, the thin plate construction is susceptible to warping due to thermal cycling at temperatures well below the softening points of the braze and plate materials. As the plates are constrained at the outside perimeter with braze material, any warp will break the brazed joint and vent fluid to atmosphere. Brazing the plates together also limits de-fouling maintenance to chemical cleaning only, which is not always effective. Despite the very attractive low cost and high effectiveness demonstrated by BPHE units, they are not suitable for use in the subject system due to operating temperatures that would severely limit service life.

5.3.2.2. Shell and tube heat exchanger

The shell and tube heat exchanger (STHE) is the most common variety of heat exchanger, accounting for 80 percent of all industrially installed exchangers in the European market [5.22]. This can be partially attributed to the versatility of the
design and due to a high degree of standardization. Such standardization allows fabrication of the STHE without requiring a costly design process. The standard most commonly used around the world is the Tubular Exchanger Manufacturers Association (TEMA); this standard is meant to augment the ASME boiler and pressure codes [5.22]. A STHE can be built by choosing from the various standardized components available under the specification, a summary of the specification is shown in Figure 5-4. STHE units are typically larger and heavier than plate fin or BPHE units, but benefit from a more robust design. For processes that require high pressure (greater than 30 bar) or high temperature (greater than 800°C), non-tubular exchangers are generally not suitable. For mobile applications such as powerplant recuperation, the prohibitively large size and weight of the STHE force designers to consider lighter and smaller alternatives. The STHE consists of a shell which determines the flow pattern within the exchanger. Different shell constructions can be used to achieve different overall heat transfer coefficients. Depending on internal baffle construction and where inlet and output ports are placed flow can be made to travel in a cross, counter, parallel, or split-flow manner.
Figure 5-4: Graphical summary of TEMA fabrication specifications [5.23]

To some extent the tube geometry is dictated by the shell geometry, however two
main variations exist: straight tube, and U-tube. While increasing the overall heat transfer coefficient is always a priority, ease of maintenance is also significant. U-tube construction offers a lighter and simpler design as only one tubesheet is required, see Figure 5-5; U-tube bundles are also easily removed for cleaning*. Compared to the straight tube, which requires two tube sheets and two removable heads, the U-tube saves on weight and cost. A penalty is paid in that the flow in a U-tube installed in a shell without a longitudinal baffle varies between parallel-, counter-, and cross-flow with a deleterious effect on overall heat transfer. Straight tube versions can choose and tightly control what method of flow arrangement is desired.

*Note that U-tube bundles can only be removed if no longitudinal baffle is present in shell construction.

For the purposes of this thesis heat exchanger selection criterion consisted primarily of cost, ease of maintenance, and service life. The STHE has the
potential to meet or exceed the maximum operating temperatures and pressures found in the modelled system, and has decades of successful industry use. Quotes from suppliers for dual pass cross-flow STHE units sized for the trigeneration system under study were obtained at an average specific cost of 60.5 CAD per kW of heat transfer [5.11]. This cost was quoted for two units, it is anticipated this price would be significantly lower for bulk orders. As the price for a suitable STHE unit is sufficiently low for small-scale applications, and the operating characteristics permit high temperature and pressure operation the STHE is ideal for use as a low temperature heat exchanger in the subject system.

5.3.2.3. Plate fin heat exchanger

The plate fin heat exchanger (PFHE) consists of a stack of alternating plates and folded fin spacers as shown in Figure 5-6. Flow is directed into the spaces between the plates provided by the fins in an alternating manner. This flow can be cross- or counter-flow. PFHE have very high area densities (heat transfer surface area per volume), which makes them ideal for compact applications [1.46][2.36][5.13]. Due to the thin wall construction of the PFHE, a differential pressure of less than 1000 kPa must be maintained; however high service temperatures upwards of 800°C can be achieved [5.13]. Because construction involves numerous brazing operations, cost can be high. Due to extensive use of
PFHE technology in the automotive industry, automation and high volume demand has significantly reduced the cost for standardized PFHE designs.

Of particular interest is the low heat capacity of PFHE units. One of the simplifications made for the model was that no transient behaviour was incorporated. With respect to a heat exchanger the lower the heat capacity, the less error introduced during load changes given that transient behaviour is not being modelled. Any energy required to warm up the exchanger results in reduced efficiency during the warm up period. Since the system being studied cycles on and off roughly every 20 minutes, such warm up periods will temporarily decrease the electrical efficiency of the microturbine. Use of PFHE designs for #1 and #3 Hx would help in reducing the required warm up time, and reach design electrical efficiency faster.

Figure 5-6: Cutaway view of a PFHE in cross-flow and counter-flow [5.13]
No price quotes or estimates could be obtained for a high-temperature PFHE unit sized appropriately for the subject system, therefore it is not possible to determine if PFHE designs are cost competitive with STHE designs. For lower HEN firing temperatures (1200 K or less), the PFHE is considered superior to the STHE however STHE designs have the potential to operate at much higher temperatures than the PFHE. Fabrication of PFHE units with ceramic materials invalidates this claim, however the cost of such a unit would most likely be prohibitively high for a small-scale user. As the option of increasing maximum cycle must be left open, the PFHE is not considered a suitable candidate to fulfill the role of low-temperature heat exchanger.

5.3.2.4. Regenerators

Regenerators are one of the most unique heat exchanger designs available today. Even though they demonstrate effectiveness in excess of 98 percent [5.26], and are compact and lightweight, cross-contamination is a problem. Figure 5-7 illustrates the challenge that exists to keep the cold and hot streams separated across a rotating component. #1 and #3 Hx exchange heat between clean air from the microturbine and combustion gases from #2 Hx. The clean air is then exhausted into the dwelling after expansion through the microturbine, therefore any cross-contamination with combustion gases is unacceptable. For
this reason regenerators cannot be used in this application.

![Diagram](image)

**Figure 5-7: A rotating matrix regenerator [5.22]**

### 5.4. Secondary compressor

Several compressor designs were considered to fulfil the role of secondary compressor. As the secondary compressor operates with a highly variable power input, it is important to select a machine that demonstrates good off-design isentropic efficiency performance. A suitable machine also has to be able to produce reasonably high flow rates to facilitate rapid accumulator charging. Three compressor styles were considered and will be compared: radial, reciprocating, and screw compressors.
5.4.1. Radial compressors

Most small gas turbines and almost all microturbines make use of radial compressors, an example of a radial compressor wheel from a turbocharger is shown in Figure 5-8. Radial machines offer high flow rates in a compact and cost-effective design, making them ideal for aerospace applications. Designed for applications with small to medium flow rates that require high RPM operation, radial machines are capable of continuous operation above 250,000 RPM is due to robust design.

Figure 5-8: Radial compressor (foreground) and axial turbine from a turbocharger [5.19].
Radial machines have traditionally demonstrated design point isentropic efficiencies of 0.75 to 0.80 at a PR of up to 4, however high-performance machines can operate at a PR up to 8 [5.19] with efficiencies in excess of 0.90 [5.20]. Unfortunately to enjoy the benefit of high compression with high efficiency a premium must be paid to achieve efficiencies in excess of 0.85. Radial machinery is therefore not considered an economical candidate for the secondary compressor.

5.4.2. Reciprocating compressors

Gas-compression applications for reciprocating compressors range from provision of shop air for air tools to providing natural gas pipeline compression. The pros and cons of reciprocating technology have been discussed in Sections 1.4.1 and 1.4.3. With respect to a small-scale application, some concerns with regard to the use of reciprocating equipment include: high operational noise, high maintenance cost, inclusion of expensive auxiliary systems. A suitable secondary compressor must not reduce the life cycle of the system as a whole; hence maintenance intervals and service life of the secondary compressor must be equal to or greater than that of the microturbine. Reciprocating compressor technology cannot meet this requirement, therefore is not considered a suitable candidate for the secondary compressor.
5.4.3. Screw compressors

Screw compressors offer a unique combination of high flow and high efficiency without special design, as shown in Figure E-9 through Figure E-11. Commercially available units, such as the model used in the simulation, demonstrated isentropic efficiencies in excess of 0.90 with single stage pressure ratios of up to 13 [5.2]. The combination of low RPM and only two moving parts (compressor rotors) allows for an expected service life in excess of 20,000 hours operating at maximum load [5.1]. While screw compressors are more expensive than reciprocating compressors, the combination of low operating noise, low maintenance costs, and availability of packaged small-scale commercial units makes the screw compressor a superior choice for small-scale users. Screw compressors also deliver high-quality discharge air with very low oil intrusion. This is particularly important as secondary compressor discharge is eventually vented into the house. As a screw compressor delivers high efficiencies, with low maintenance, low operational noise, and a long service life, it makes an ideal candidate to fill the role of secondary compressor for this study.
Figure 5-9: Cutaway view of a screw compressor used in a high-performance supercharger [5.6].
Chapter 6
Conclusion

6.1. Summary

Severe weather, greenhouse gases, and energy tariff fluctuations have typically not been primary concerns of individual consumers when making decisions regarding energy needs in the 20th century; this will not be the case in the 21st century. With the dawn of rolling blackouts due to insufficient power grid capacity, communities becoming isolated due to inclement weather, and rising energy prices new solutions for small-scale users are becoming increasingly important to meet future energy needs. Several ingenious small-scale solutions that reduce energy consumption and decrease dependence on grid power have been in use for many years. Heat pumps, geothermal heating and cooling, and thermal storage systems have proven to be effective at providing thermal control for residential and small commercial customers alike. These solutions are still at the mercy of disruptions in grid power service. Each system has problems that prevent widespread acceptance; for example, heat pumps do not work well in extreme cold and geothermal heating cannot be installed in northern communities where disruption of the permafrost layer results in geological instability. No system currently exists in practice that can provide the option of complete energy islanding for the small-scale user. To meet these challenges, this study was initiated to design and model a trigeneration system capable of on-
site production of heating cooling and power.

Large trigeneration systems have been successfully implemented for industrial purposes; they work well and are thoroughly documented. These systems have not filtered down to small-scale users in part due to the use of chilling equipment with very high specific capital cost. A successful small-scale trigeneration system must compete with the most efficient form of individually providing heating cooling and electric power via a natural gas furnace, vapour compression air conditioner, and grid power. A successful small-scale trigeneration system will demonstrate the following qualities: a long service life with minimal maintenance requirements, autonomous operation, low capital costs to compete with individual generation systems, and operating costs competitive with individual generation.

A new trigeneration system was proposed to satisfy these requirements for a small-scale application. An indirectly fired microturbine was combined with energy storage in the form of a hydraulic accumulator. The accumulator was used in an inverse Brayton cycle in combination with a microturbine to provide for all heating cooling and peak power needs for a typical detached single-family dwelling. To ensure capital costs stay as low as possible, state-of-the-art turbomachinery and heat exchangers were not used in modelling and simulations. This produced conservative results that provide for additional studies. Performance data for the proposed system was mathematically modelled using MATLAB™. This model was then incorporated into a time-based
SIMULINK™ simulation, using modelled energy load profiles for a typical household located in central Canada. The simulation provided control to ensure a comfortable household temperature was maintained, and electrical demands were satisfied. The simulation was used to measure economic performance and to identify areas of future improvement in the system. Microturbine design and off-design performance data was validated against performance data from GASTURB™, commercially available microturbines, and simulated systems discussed in open literature, and were found to be in good agreement. The accumulator model was verified against experimental data for both charging and discharging. As pressure and temperature of the experimental and modelled accumulators were in agreement once fully charged or discharged, the model maintained conservation of mass.

After experimenting with various system modifications in an effort to improve economic performance, a final configuration was arrived at which operates in two modes; one for heating and one for cooling load production. This configuration uses a secondary compressor and expander in addition to the indirectly fired microturbine and accumulator. An additional heat exchanger (#4 Hx) was used in addition to the heat exchangers installed as part of the indirectly fired microturbine assembly. The #4 Hx is buried in-ground to take advantage of the year round pseudo-infinite heat capacity offered by deep ground installation.
6.2. Summary of results

The effect of varying accumulator size on system performance was investigated. It was determined that accumulator size has negligible impact on economic performance. Size variation did have an effect on cycle frequency, with smaller sizes decreasing the period between successive microturbine starts. Accumulator size was therefore determined to only have an impact on system life and durability. Larger sizes were found to reduce system cycling; this is expected to increase component life and reduce maintenance costs. Selection of an appropriate size should also be based upon practical considerations such as ease of installation, cost, and microturbine cycling limitations.

Different HEN modes were used for heating and cooling load production. Mode 1 was designed to ensure a high microturbine exhaust temperature of 860 to 880 K (depending on ambient temperature) was delivered for household heating purposes. A thermal efficiency of 15.7 percent and total efficiency of 95 percent was achieved at ISO standard atmospheric conditions for Mode 1. Mode 2 was designed to maximize the thermal efficiency of the microturbine while producing a cooling load. Since high-temperature exhaust was not required, a thermal efficiency of 29.3 percent was achieved at ISO standard atmospheric conditions. Microturbine size had a negligible effect on economic performance. Microturbine size determined how fast household temperature was recharged during heating mode, and how fast the accumulator was recharged during cooling mode. In combination with accumulator size, microturbine size determined the period
between successive starts. To achieve energy islanding during heating mode, a minimum engine size was required to satisfy peak household electrical demand. An oversized engine should be avoided as well to avoid excessive household heating mass flows and increased capital costs. Factors influencing microturbine selection therefore include capital cost, household electrical load, and household thermal load. A microturbine with 10 kWe output at standard conditions was selected.

Two different methods to charge the accumulator were investigated. The first method attempted to use the microturbine to simultaneously provide electrical load and charge the accumulator. By extracting varying levels of compressor bleed flow, the microturbine could be operated in an electrical load following manner. The second method used a separate compressor to charge the accumulator. Electrical input was fed to the secondary compressor from a microturbine that operated at full power. Using bleed flow consumed 4 percent more fuel when compared to use of a secondary compressor when operating in Mode 1. If bleed flow is used in Mode 2, the system could not provide a cooling load greater than 0.75 kWt, while a cooling load of up to 2 kWt was provided with a secondary compressor without supplemental electrical power. The addition of a secondary compressor also provided the option of using grid power to increase the cooling capacity of the system. A secondary compressor was incorporated into the final configuration to benefit from the reduced fuel costs, and to provide
sufficient cooling load during peak summer months.

The effect of using an in-ground heat exchanger (#4 Hx) to increase the thermal output of the accumulator was studied. Cooling secondary compressor flow in an in-ground heat exchanger before discharge to the accumulator reduced system operation costs by up to 72 percent for high cooling load conditions. This reduction in cost can be attributed to a significant increase in specific cooling capacity of expander discharge flow with cooler accumulator temperatures. Pre-heating secondary compressor inlet flow in the in-ground heat exchanger had a negligible effect on system operational costs; therefore the in-ground heat exchanger was used for Mode 2 only.

To increase specific work output from the expander when operating as part of the inverse Brayton cycle in Mode 1, accumulator discharge was cycled through the heat exchanger network to raise expander inlet temperature to design point levels. Fuel costs were reduced by 9 percent when firing the HEN at a constant design temperature of 1200 K.

It was found that if the microturbine expander was used as part of the inverse Brayton cycle in Mode 1, thermal output often exceeded household demand. If household temperature was not allowed to cool down during inverse Brayton cycle operation, microturbine exhaust had to be dumped overboard to prevent
household temperature from exceeding setpoint limits; which reduced system economic performance. A second expander 1/6th the size of the microturbine expander was added to modify the thermal output of the inverse Brayton cycle. This ensured household thermal demand was not exceeded. The smaller second expander permitted the HEN to be operated at maximum temperature during IBC operation for maximum economic performance, without exceeding the household thermal load.

The independent generation system was found to be 48 percent cheaper to operate based on one year of operation in Winnipeg, Canada when compared to the trigeneration system. Economic performance was compared for regions around the world with similar climates to central Canada. As the ratio of electricity tariffs to natural gas prices were relatively constant throughout the regions investigated, economic performance demonstrate minor variation; independent generation was found to be between 35 and 47 percent cheaper to operate when compared to the trigeneration system. This was not the case for countries in the former Soviet Union, where the combination of extremely low natural gas prices and relatively high electricity prices result in the trigeneration system being 20 percent cheaper to operate when compared to the independent system, based on one year of operation.
6.3. Conclusions

The preliminary design and simulation of a small-scale trigeneration system was successfully completed with promising results and provided direction for future studies. Preliminary designs indicate that the system can be built using a combination of modifying existing technology, and off-the-shelf components such as shell and tube heat exchangers. Despite the lower than expected economic performance of the system in Mode 2, there is much room for optimization and improvement. The results obtained represent a conservative prediction of performance, and can be improved upon with future system designs. Economic performance while providing a heating load was predicted to be marginally higher than an independent generation system.

It was a goal of this project to create a system that offered total energy islanding to small-scale consumers. The results show that if peak summer thermal loads are to be satisfied, connection to a grid is required. The trigeneration system is capable of supplying continuous cooling loads of about 2 kWt or less. For the climate in the geographical region used for load prediction (central Canada), cooling loads exceeded 2 kWt only 5 percent of the year. This means total energy islanding was achieved for 95 percent of the year. Energy islanding for the full year is possible if any of the following criteria are satisfied: 1) the region has mild cooling demands, 2) the household setpoint temperature is raised during summer months, 3) improvements to the trigeneration system increases cooling capacity.
Perhaps what is most promising about the trigeneration system is that there is no other product being simulated, tested, or made available for purchase that can satisfy the same load demands. Trigeneration has not yet been brought to the small-scale consumer in an economical manner that permits energy islanding, leaving no current solution for a growing niche market. Energy islanding is an attractive option for mobile and remote users, and provides a solution for those dissatisfied with frequent power outages. It is difficult to place an economic value on the intrinsic benefit of energy islanding, as this value will change from user to user. For some users, operating a household free from grid power may justify the increased fuel costs associated with the subject trigeneration system. Despite demonstrating inferior economic performance when compared to the independent generation system, the subject trigeneration system still has much to offer.

6.4. Future work

A sensitivity study should be performed to investigate the effect component isentropic efficiencies have on economic performance. Such a study has the most impact on cooling load production, which requires as much energy to be extracted from microturbine flow as possible to increase electrical efficiency.

Increasing HEN maximum temperature was found to increase microturbine electrical efficiency, however as no suitable high-temperature heat exchanger with integrated burner exists in the size required, a realistic maximum
temperature is unknown. Research and testing are required to be able to estimate maximum HEN temperatures with accuracy.

Further work is required to increase the accuracy of the accumulator model. As estimates of heat transfer coefficients are highly empirical, the heat transfer coefficients used in the simulation are not calibrated for the application. Removing isothermal and isobaric assumptions will also improve accumulator behaviour prediction.

There is potential for improvement to system economic and thermodynamic performance with the incorporation of water injection. This system could also be used to maintain household humidity levels year round. Simulation is required to investigate if such a system would justify the increased capital cost.

The simulated trigeneration system must be prototyped to confirm simulation predictions with confidence. The simulation could then be modified and used to predict system performance due to subsequent modifications with a higher degree of confidence.
References

CHAPTER 1


[1.29] Personal files from experience at Air Canada Technical Services, 2006.


CHAPTER 2


[2.5] Bassols, J. Kuckelkorn, B., Langreck, J., Schneider, R., Veelken, H.,


Chapter 3


Chapter 4


Chapter 5


[5.2] Aerzen USA Corporation, VMX0a37R screw compressor performance


**Appendix E**


Appendix A
Experimental small-scale CHCP apparatuses

The following are some photographs of experimental small-scale trigeneration apparatuses discussed in open literature.

Figure A-1: Experimental CHCP using a VCR unit [1.26]
Figure A-2: Experimental CHCP using an ACR unit [1.20]

Figure A-3: Experimental CHCP using an ACR unit [2.18]
Lighting and occupant gains were automatically calculated by the ESP-r program based upon typical habits of a four-person family. Equipment gains included heat output from a refrigerator, latent heat gains from showers and baths, latent and sensible heat gains from cooking on a stove or oven, and sensible heat output from computer equipment.

**Figure B-1:** Typical Canadian ground temperature profile imposed on exterior of ground surface of 1st floor. Data taken from standard profiles included in ESP-r
Figure B-2: Occupant driven gains for 1st floor of ESP-r model

Figure B-3: Occupant driven gains for 2nd floor of ESP-r model
Figure B-4: Lighting gains for 1st floor of ESP-r model

Figure B-5: Lighting gains for 2nd floor of ESP-r model
Figure B-6: Equipment gains for 1st floor of ESP-r model

Figure B-7: Lighting gains for 2nd floor of ESP-r model
Figure C-1: Compressor map for the Garrett GT22 series turbocharger
Downloaded from www.turbobygarrett.com on Dec. 2 2007
Figure C-2: Expander map for the Garrett GT22 series turbocharger
Downloaded from www.turbobygarrett.com on Dec. 2 2007
Appendix D
Capstone microturbine standard maintenance schedule

C60 and C65 Gaseous Fuel Systems Scheduled Maintenance
C60 and C65 gaseous fuel systems scheduled maintenance intervals apply to Model C60, C65, and ICHP High Pressure Natural Gas systems. Maintenance items and intervals for the various components of these systems are highlighted in the following table.

<table>
<thead>
<tr>
<th>Maintenance Interval</th>
<th>Component</th>
<th>Maintenance Action</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>24 months</td>
<td>UCB Battery</td>
<td>Replace</td>
<td>See Note 1</td>
</tr>
<tr>
<td>4,000 hours</td>
<td>Engine Air Filter</td>
<td>Inspect</td>
<td>Replace if application requires - see Note 2</td>
</tr>
<tr>
<td></td>
<td>Electronics Air Filter</td>
<td>Inspect</td>
<td>Clean if necessary - see Note 2</td>
</tr>
<tr>
<td></td>
<td>Fuel Filter Element (External)</td>
<td>Inspect</td>
<td>Replace if application requires - see Note 2 (Not required for Gas Pack)</td>
</tr>
<tr>
<td></td>
<td>Fuel System</td>
<td>Leak Check</td>
<td>Refer to &quot;Gaseous Fuel Fittings and Components&quot; section below for recommended procedure</td>
</tr>
<tr>
<td>8,000 hours</td>
<td>Engine Air Filter</td>
<td>Replace</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Electronics Air Filter</td>
<td>Clean</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Fuel Filter Element (External)</td>
<td>Replace</td>
<td>Not required for Gas Pack</td>
</tr>
<tr>
<td></td>
<td>Igniter</td>
<td>Replace</td>
<td>See Note 3</td>
</tr>
<tr>
<td></td>
<td>ICHP Actuator</td>
<td>Replace</td>
<td></td>
</tr>
<tr>
<td>20,000 hours or 3 years</td>
<td>Battery Pack</td>
<td>Replace</td>
<td>Refer to Battery Tech Ref (410044) for expected life vs duty cycle, and &quot;Battery Maintenance During Storage&quot; section below for recharge intervals</td>
</tr>
<tr>
<td>20,000 hours</td>
<td>Injector Assemblies</td>
<td>Replace</td>
<td></td>
</tr>
<tr>
<td></td>
<td>TET Thermocouple</td>
<td>Replace</td>
<td></td>
</tr>
<tr>
<td></td>
<td>SPV</td>
<td>Replace</td>
<td>Replace with Woodward Valve Upgrade Kit</td>
</tr>
<tr>
<td>40,000 hours</td>
<td>Electronic Components: ECM, LCM &amp; BCM Power Boards, BCM &amp; ECM Fan Filters, Fans, EMI Filter, Frame PM</td>
<td>Replace</td>
<td>Kits available for each major configuration</td>
</tr>
<tr>
<td></td>
<td>Engine</td>
<td>Replace</td>
<td>Use Reman or New Engine Replacement</td>
</tr>
</tbody>
</table>

Figure D-1: Excerpt from Capstone Turbines scheduled maintenance work instructions for the 60 kWe C60 and C65 models. Obtained via personal communication with Dan Lubell, chief turbomachinery engineer with Capstone Turbines.
Appendix E
Component Performance Validation

Accumulator

To verify the results obtained from the accumulator model, experimental data was gathered from a simple accumulator apparatus illustrated in Figure E-1. The accumulator was charged from shop pressure at 90 psi, and then discharged to ambient through a ¼" orifice.

Figure E-1: Experimental accumulator apparatus

The accumulator model was modified to mirror the test apparatus:
• no insulation was used
• ambient temperature was set at a constant 18°C
• mass flow during discharge and charging of the test apparatus was calculated from temperature and pressure readings and then used as a mass flow vs. time profile for the accumulator model

![Figure E-2: Comparison of modelled accumulator (n=1.2) and experimental results during discharge](image)

Figure E-2 and Figure E-3 show good agreement for pressure. Note the different values of the polytropic coefficient n used for discharging and charging. It was
found that assuming isothermal \((n = 1)\) compression for the charging example was valid as the process was completed over a long time. This assumption was not valid for discharging, as the time for complete discharge was about half of the charging period.

Conversely, assuming a completely isentropic process \((n = 1.4)\) did not produce

Figure E-3: Comparison of modelled accumulator \((n=1)\) and experimental results while charging.
good agreement either. These results illustrate the need to tailor the polytropic coefficient depending on rate of discharge or charging. The simulation uses a polytropic exponent of 1.4 as the charging and discharge period is most often less than 100 seconds; at peak electrical demand the accumulator can discharge in less than 30 seconds.

![Graph](image)

Figure E-4: The effect of heat transfer on modelled accumulator behaviour with zero flow. Exterior insulation is glass fibre (0.038 W/mK) and is 10 cm thick.

Good agreement was not achieved for temperature. This is believed to be a
combination of two factors. Heat transfer calculations for the model are for a horizontal cylinder and are based upon empirical correlations for convection coefficients that are a best guess; actual convection coefficients are most likely much higher. Flow temperature is also recorded at the end of a 1 m long, 0.0508 m (2 in.) diameter pipe rather than in the accumulator (as seen in Figure E-1). Residence time for flow in the pipe was on average about 1 second for the blowdown period. Combined with a large wetted area, this makes for a high rate of heat transfer between the accumulator and the temperature measuring point.

As the disagreement in temperature is believed to be a result of heat transfer to ambient not accounted for in the model, it is anticipated that if the test apparatus was well insulated this discrepancy would be negligible. Mass is conserved during discharge, as the final temperature and pressure readings agree. Temperature data was not measured during charging, as there was no provision to measure the accumulator temperature; measuring pipe flow temperature did not provide any information as there was no flow in the pipe during charging. Therefore there is no comparison available for accumulator temperature during charging.

Figure E-4 is an example of the effect of heat transfer on the accumulator with zero flow. The accumulator was charged at a high temperature and then allowed
to remain static, with no discharge or charging flows to observe the temperature and pressure drop over time. Ambient air was set at 22°C. The accumulator took roughly an hour to equalize its temperature with ambient. This result shows that heat transfer has a negligible effect on IBC performance if the accumulator is discharged and charged frequently. During low load periods, there is greater potential for heat loss or gain to occur.

Microturbine
The trigeneration system under study is complex, involving off-design component matching, over a wide range of operating conditions. To have a measure of confidence in the results obtained from the simulation, verification of the model is required. A good place to start is by looking at IFGT performance at design.

Design point performance
As the trigeneration model is based upon component maps generated from GASTURB™, external validation is required in addition to using GASTURB™ to validate in-house model performance. A team from the Lappeenranta University of Technology has designed an IFGT CHP microturbine system fueled by biomass (wood, corn, etc..) for a medium sized commercial application as shown in Figure E-5; this system will be referred to as the bio-IFGT system. The bio-IFGT system differs in how the heat load is provided and in the fuel used, however the heat exchanger configuration is similar to what is used for Mode 1.
The presence of a HSRB and use of bio-fuels does not allow a fair comparison of total efficiency between the two systems, however these differences have negligible impact on power output given the similar heat exchanger configuration. Table E-1 compares design performance of the trigeneration model with the output from GASTURB™ and the performance of the bio-IFGT configuration. In order to make a fair comparison, parameters in the GASTURB™ and
trigeneration models were modified to match those used in the bio-IFGT simulation. They are as follows:

- $\eta_c = 0.84$
- $\eta_e = 0.83$
- $\Delta P_{\text{exhaust}} = 9\%$
- $\Delta P_{\text{hx}} = 4\%$
- $EIT = 1223\, K$
- $LHV = 10.459\, MJ/kg$
- $\eta_m = 0.98$
- $\dot{W} = 80\, kWe$

The results, tabulated in Table E-1, show good agreement for all three simulations. GASTURB™ does not have an option to model the burner section of a gas turbine as a series of heat exchangers. The effect is similar to specifying heat exchangers with 100 percent effectiveness. As a result, the GASTURB™ simulation predicted a high thermal efficiency. Even though the thermal efficiencies do not match, it is expected the trigen system should have a lower predicted value. With an HEN effectiveness of unity, the thermal efficiency of the trigen system increases, shown in Table E-1. The bio-IFGT model used an in-house heat exchanger heat transfer model that made use of the log mean
temperature difference method to more accurately predict HEN performance. Use of effectiveness parameters by the in-house model and the GASTURB™ simulation is a simplification that introduces error. The discrepancy in thermal efficiency between the bio-IFGT system and the trigen system is inferred to be due to the different methods of modelling heat exchanger heat transfer.

Table E-1: Comparison of design point performance of Mode 1 at standard atmospheric conditions for several similar microturbine IFGT cycles

<table>
<thead>
<tr>
<th></th>
<th>Specific Power Output (kJ/kg)</th>
<th>Thermal Efficiency (percent)</th>
<th>PR</th>
<th>TIT (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Trigen system</td>
<td>143.4</td>
<td>19.5</td>
<td>4</td>
<td>1223</td>
</tr>
<tr>
<td>Trigen system $\varepsilon = 1$</td>
<td>143.2</td>
<td>19.9</td>
<td>4</td>
<td>1223</td>
</tr>
<tr>
<td>GASTURB™ single spool</td>
<td>146.8</td>
<td>21.3</td>
<td>4</td>
<td>1223</td>
</tr>
<tr>
<td>Bio-IFGT [E.4]</td>
<td>145.0</td>
<td>17.8</td>
<td>4</td>
<td>1223</td>
</tr>
</tbody>
</table>

Modelling Mode 2 in GASTURB™ differed from Mode 1 in that combustion flow is pre-heated by expander exhaust. This effect is approximated in GASTURB™ with the use of a recuperator that exchanges heat between expander exhaust and compressor discharge flow. #1 and #2 Hxs are treated as ‘black boxes’ in the same manner as was done for Mode 1. This is accomplished by specifying a TIT and combustor pressure loss that is equal to what the HEN delivers in the
mathematical model. Again the CHCP system and GASTURB™ simulations were in agreement to within about 2 percent on key performance parameters as shown in Table E-2. The IFGT-Rec-Rec (IFGT double recuperated) system, shown in Figure E-6, shares the same HEN design as the trigen system but operates at a lower TIT and PR.

Table E-2: Comparison of design point performance of Mode 2 at standard atmospheric conditions for several similar microturbine IFGT cycles

<table>
<thead>
<tr>
<th></th>
<th>Specific Power Output (kJ/kg)</th>
<th>Electric Efficiency (percent)</th>
<th>PR</th>
<th>TIT (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Trigen system</td>
<td>113.0</td>
<td>30.6</td>
<td>4</td>
<td>1163.4</td>
</tr>
<tr>
<td>GASTURB™ Single spool</td>
<td>111.6</td>
<td>29.9</td>
<td>4</td>
<td>1163.9</td>
</tr>
<tr>
<td>recuperated</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>IFGT-Rec-Rec [E.1]</td>
<td>94.3</td>
<td>22.0</td>
<td>3</td>
<td>1150</td>
</tr>
<tr>
<td>Ingersoll-Rand PowerWorks 250 [E.5]</td>
<td>135.9</td>
<td>32</td>
<td>4.1</td>
<td>1200</td>
</tr>
<tr>
<td>Capstone C30 [E.5]</td>
<td>96.8</td>
<td>26</td>
<td>3.5</td>
<td>1113</td>
</tr>
</tbody>
</table>

It is therefore expected that the efficiency and specific power is lower than the trigen system. The two other systems included in Table E-2 are commercially available microturbine CHP units. While no system described in Table E-2 matches CHCP system performance (except for GASTURB™), the trend of low PR and low TIT corresponding to lower efficiency and specific power output (or
vice versa) is consistent with the results obtained from the CHCP system model. For example, the Ingersoll-Rand package has a slightly higher TIT and PR when compared to the CHCP system, and has a corresponding slight increase in specific power and efficiency.

Figure E-6: Schematic of the IFGT-Rec-Rec system

**Off-design performance**

Microturbine performance was compared against output from GASTURB™ for all
possible outside air temperatures, and for power settings that were varied from maximum HEN temperature (maximum power) to synchronous idle along a line of constant speed. Good agreement was obtained throughout the operating envelopes for both Mode 1 and 2, as shown in Figure E-7 and Figure E-8.

![Figure E-7: Comparison of output from GASTURB™ and the in-house model for Mode 1 for various ambient temperatures](image-url)
Secondary compressor

Performance throughout the full range of possible flow rates and delivery pressures for the secondary compressor was modelled using actual performance data from a commercially available compressor. Flow and power versus RPM charts from the Aerzen Maschinenfabrik corporation's VMXa037R screw compressor, shown in Figure E-9 and Figure E-10, were digitized then used to create functions relating mass flow and pressure rise to isentropic efficiency.
Figure E-9: Power as a function of RPM for the VMXa037R screw compressor at ISO standard atmosphere, digitized from sample maps [E.1].

The power consumption shown in Figure E-9 takes into account the efficiency of the driving electric motor and any mechanical efficiency associated with the compressor drivetrain. The efficiency calculated from the charts is therefore not a true isentropic efficiency, as it incorporates the motor efficiency as well. This is actually preferable for ease of integration with the simulation, as the actual power consumption of the compressor motor is required rather than the power input to the compressor.
Figure E-10: Flow rate as a function of RPM for the VMXa037R screw compressor at ISO standard atmosphere, digitized from sample maps [E.1].

Figure E-11: Isentropic efficiency curves for lines of constant pressure rise for the VMXa037R compressor, calculated from Figure E-9 and Figure E-10.
In an ejector cooling system, as shown in Figure F-1, refrigerant pressure and temperature is increased through heat addition provided by waste exhaust from the CHP cycle. The vapourized refrigerant then flows into a convergent-divergent ejector where liquid refrigerant is entrained into the suction area through the secondary entrance, shown in Figure F-2.

Figure F-1: Schematic of an ejector cooling cycle as part of a CHCP system [2.12].

The vapour and liquid refrigerant mix in the constant-area throat section, and
then experience an increase in pressure and reduction in temperature associated with transition through a shock as the flow passes into the diffuser. The refrigerant then enters the condenser where it is returned to a liquid state. Cooling load is provided by high-pressure refrigerant passing through the evaporator.

![Diagram of an ejector](image)

Figure F-2: Cross-section of an ejector [2.12].